

Broadband Single-layer E-Patch Reflectarray

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Abstract. *E-shaped patch resonator is proposed for designing a novel broadband linearly polarized reflectarray for the first time. The element is made up of a shorted E-shaped patch with a polystyrene foam placed beneath it, and no dielectric substrate is needed in the reflectarray design. The unit element is simulated using Floquet method and it is found that a reflection phase range of $\sim 360^\circ$ is easily obtainable by varying the arm length of the shorted E-shaped patch. A full 11×11 reflectarray has been designed to achieve an antenna gain of ~ 23.7 dBi and a -1 dB gain bandwidth of 8.1%. The cross-polarization is found to be ~ 18 dBi smaller than its co-polarization in the boresight direction. The proposed reflectarray is simple to design as it requires the use of only a single layer.*

Keywords

Reflectarray, shorted E-shaped patch, linearly polarized reflectarray

1. Introduction

The first reflectarray, which was constructed using an array of truncated waveguides, was introduced by Berry et al. in 1963 [1]. Nevertheless, such waveguiding structure is nonplanar and bulky. It was followed by the implementation of microstrip reflectarray which is consisted of multiple patch elements of varied size [2]. Although microstrip structure is planar, its conductor and dielectric losses at high frequencies can be severe and the achievable bandwidth is usually narrow. Over the years, much effort has been made to enhancing the bandwidth of microstrip reflectarrays. Multilayer technology has been proven to be the one of the popular alternatives that can effectively extend the bandwidth [3]. Exploration on broadband microstrip reflectarray elements continues because of the possible applications of the microstrip reflectarrays in the space-related applications. Unit elements such as double hexagonal rings [4], disk element with attaching phase-delay lines [5], [6], triple square rings [7], and square patch with dual gap [8] were discovered to be able to produce broad frequency bandwidth. Although the single-layer reflectarray in [9] was able to achieve wide bandwidth in

two passbands, optimization of the element was very tough and time consuming as six degrees of freedom were required when designing the unit element. Lately, active elements such as varactor diode, capacitor, and amplifier are incorporated into reflectarrays so that they are able to perform beam steering [10], and provide dual polarization [11] and amplification [12].

Reflectarray elements that are able to produce wide phase range have also been of great interest recently, although a full cycle of phase angle (360°) is usually considered sufficient for designing a full-fledge reflectarray of any size. Having an S-curve with broad phase range and slow gradient is still much sought after to make the geometrical dimension of the element more distinguishable in the design. A variety of resonators have been explored for broad phase range on a single layer. It was found that a reflection phase range of greater than 360° was easily obtainable by cascading multiple hexagonal rings [4] concentrically. Dipole was used for reflectarray design in [13], [14], and it was found that placing a couple of dipolar strips in parallel had made possible linear phase response with a phase range of more than 360° .

The E-shaped patch resonator was proposed for wireless communication applications [15–17] in the early 20s. Involvement of E-shaped patch was found to be able to achieve wide bandwidth performance. Such resonator is simple to design and its geometrical parameters can be easily optimized to achieve different specifications. In [18], it was found that dual-band performance could be realized when a U-slot patch was stacked on top of another E-shaped patch with an air layer introduced in between. Integrating the E-shaped patch antenna with an LC circuit was found useful for bandwidth improvement [19]. When deployed as transmitarray element, it requires 3 layers of identical E-shaped patches to achieve a transmission phase range of 270° [20], which is usually not sufficient for designing a full-fledge reflectarray. To our best knowledge, so far, no work is found on the use of E-patch resonator for reflectarray design.

In this paper, the E-shaped patch is used for designing a linearly-polarized (LP) broadband reflectarray for the first time. In the proposed design, the two arms of E-shaped patch are varied to generate a broad phase range of greater than 360° . To begin, the configuration of the pro-

posed reflectarray element is first described in Sec. 2. Floquet method will be used for simulating the reflection characteristics of the proposed reflectarray element. In Sec. 3, the design guideline of the full-fledge reflectarray will be explained. A prototype has been fabricated and measurement is conducted to substantiate the simulated results. A full description of the measurement setup is provided in Sec. 4, following with discussion of the measured and simulated results in Sec. 5. To study the effects of some of the crucial design parameters on the reflection characteristics and radiation performances of the proposed reflectarray, a complete parametric analysis is given in Sec. 6. The proposed unit element has a single-layer structure and it can be used for designing a large-scale reflectarray as it is able to provide a full reflection phase range.

2. Reflectarray Unit Cell Configuration

The configuration of the proposed unit element is shown in Fig. 1(a) and (b). It consists of an E-shaped metal patch etched on the top surface of a piece of square polystyrene foam ($L \times L$) with dielectric constant of $\epsilon_r \sim 1$ and thickness of $h = 4$ mm. The bottom surface of the foam is laminated with ground plane. The center arm of the E-shaped patch is shorted to the ground through via (diameter of d). With reference to Fig. 1(a), the shorting via is positioned at a distance, s from the edge of the arm. To analyze its reflection properties, the proposed element with a cell size of $25 \text{ mm} \times 25 \text{ mm}$ ($L \times L$) is simulated using the CST Design Studio. In simulation, as shown in Fig. 2, the proposed element is placed at one end of a square Floquet cell at a distance of 76 mm (in this case) from the wave port at another end, where a y -polarized plane wave with an incident angle of $\theta = 20^\circ$, $\phi = 0^\circ$ is launched. Since the reference plane is always de-embedded to the top surface of the unit element, the distance between the port and element does not affect the reflection coefficient much. With reference to Fig. 2, the top and the bottom surfaces of the Floquet cell are defined to be perfect-electric-conductor (PEC) walls while perfect-magnetic-conductor (PMC) walls for the two side walls. In order to take the mutual coupling mechanism between the elements into account, the unit element inside the Floquet cell is simulated as an infinite periodic array repeating itself. Figure 3 shows the reflection phase ($\angle S_{11}$) curves at frequencies of 7.5 GHz (0.625λ), 7.7 GHz (0.642λ), 7.9 GHz (0.658λ) and 8.1 GHz (0.675λ). With reference to the same figure, by varying the two arms (L_1) of the E-patch L_1 from 5 mm to 18 mm , a reflection phase range of $\geq 360^\circ$ can be easily obtained at the frequencies of 7.9 GHz and 8.1 GHz . In this case, the reflection phase slope at 7.9 GHz is selected for designing reflectarray. The reflection loss is not shown as it is less than 10^{-4} in the entire range. The arm widths (W_1 , W_3) and gaps (G_1 and G_2) are made to be equal (3 mm). Other design parameters are $W_2 = 2 \text{ mm}$, $L_3 = 3 \text{ mm}$, $L_2 = 7 \text{ mm}$, $s = 3 \text{ mm}$ and $d = 1 \text{ mm}$. The current distribu-

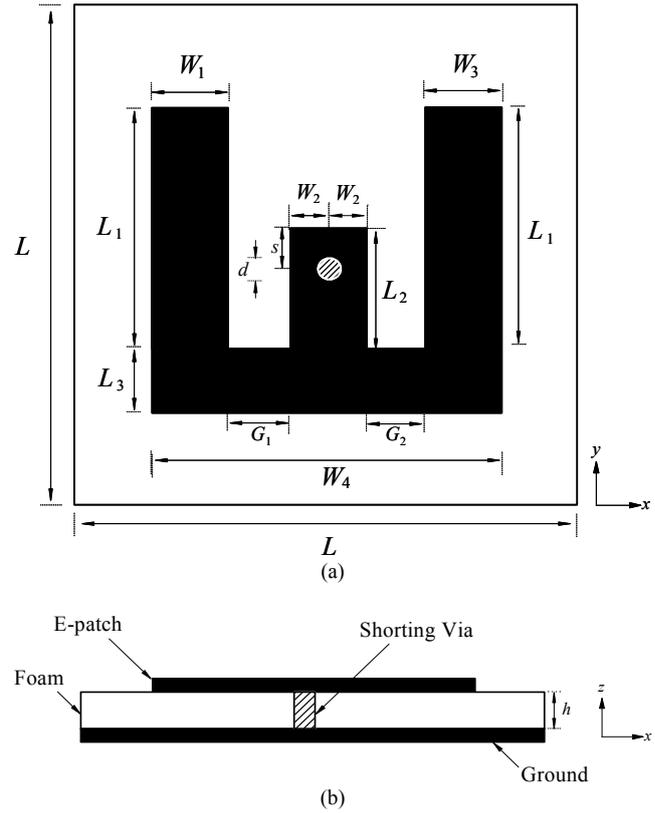


Fig. 1. (a) Top view. (b) Side view of the proposed E-patch unit element.

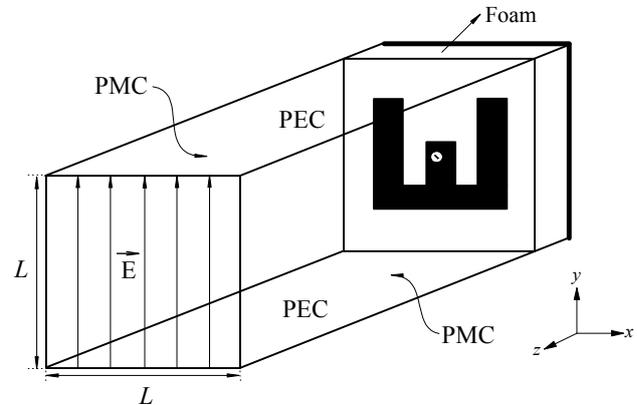


Fig. 2. Simulation setting for the proposed unit element inside a Floquet cell.

tions for the case of $L_1 = 12 \text{ mm}$ are plotted on the patch in Fig. 4(a), and the corresponding electric fields in the cavity region between the patch and ground are depicted in Fig. 4(b). Typical current and field distributions for E-patch have been observed in both, comparable with those in [16]. To show the advantages of using the E-shaped patch, a rectangular patch element, with similar size and thickness, is designed and simulated at the same frequency. To begin, a unit element which consists of a rectangular patch on the top surface of a piece of square polystyrene foam ($25 \text{ mm} \times 25 \text{ mm}$) with dielectric constant of $\epsilon_r \sim 1$ and thickness of 4 mm is designed. The bottom surface of the foam is laminated with ground plane. The rectangular patch has a width W_p of 16 mm and its length (l_p) is varied

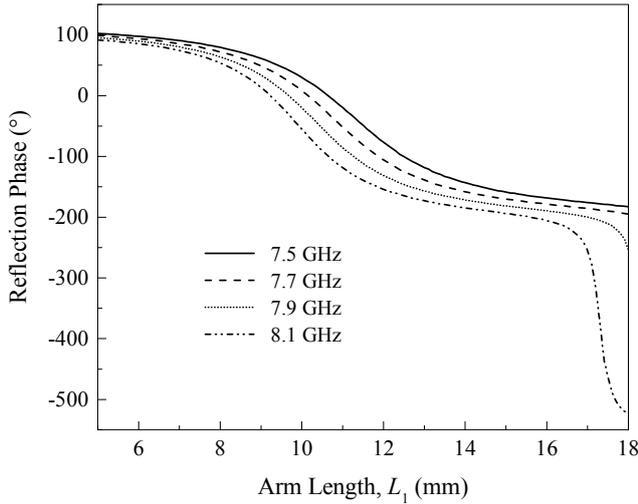


Fig. 3. Reflection phase response as a function of arm length (L_1) of the proposed element at different frequencies

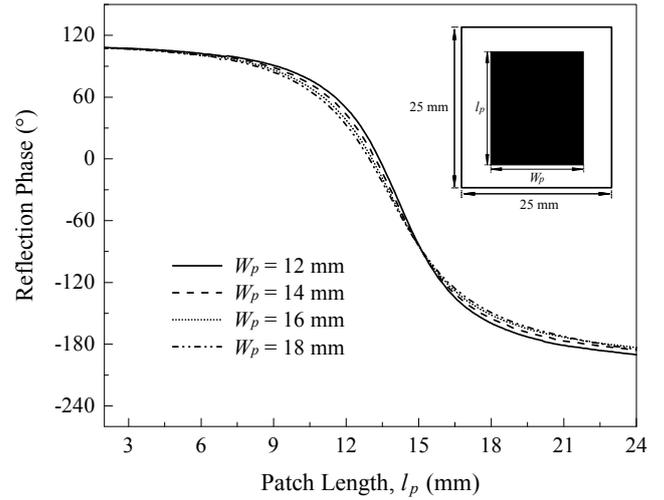
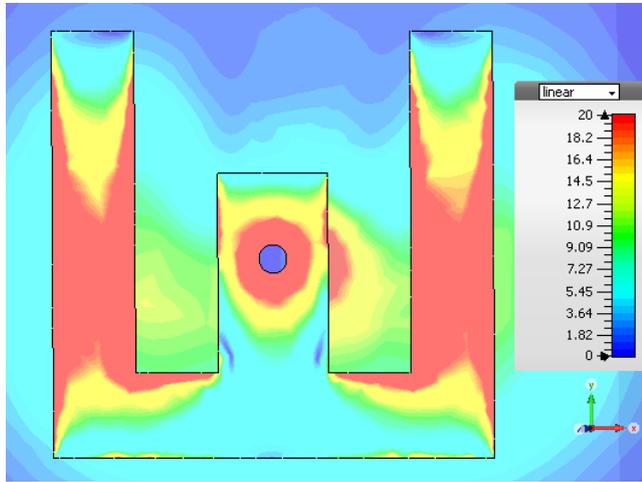
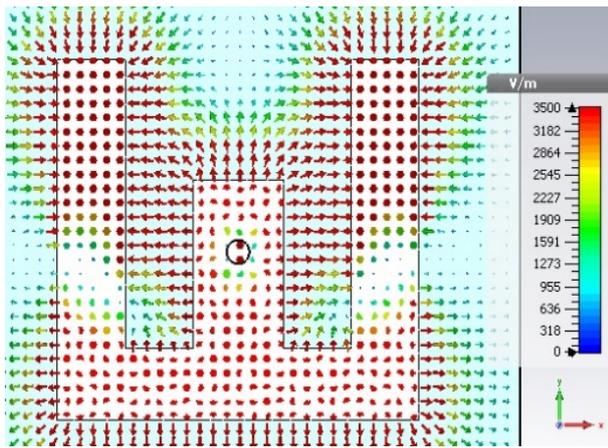


Fig. 5. Reflection phase responses as a function of patch length (l_p) of the rectangular patch element with different patch widths (W_p).



(a)



(b)

Fig. 4. (a) Surface current on the E-shaped patch, and (b) electric field distribution in the cavity region between the patch and ground for the case of $L_1 = 12$ mm.

from 2 mm to 24 mm for generating phase shift. By varying the length of the rectangular patch, a reflection phase range of 292° at 7.9 GHz is achievable, as shown in Fig. 5. With reference to the same figure, the effects of the

width (W_p) of the rectangular patch on the reflection phase are also studied. It is observed that the total phase range remains unchanged when the width (W_p) is varied from 12 mm to 18 mm, with almost the same gradient obtained for all curves. For all widths, the reflection losses are neglected as there are much smaller than 10^{-4} across the varied dimension.

3. Full Reflectarray Configuration

With the use of the phase-length curve (also called S-curve) in Fig. 3, an 11×11 linearly polarized (LP) reflectarray is designed. The elements are put into an array (shown in Fig. 8), and the locations of the elements are represented as (m, n) . The arrays are fed by a C-band pyramidal horn (5.85 GHz–8.2 GHz), which has a simulated antenna gain of 11.4 dBi in both E - and H - planes at 7.9 GHz and the horn patterns can be modelled using $\cos^q(\theta)$ where $q = 6.85$ in this case. The 3-dB beamwidth of the C-band horn in E - and H - planes are 51.6° and 47.4° , respectively, as depicted in Fig. 6. It is suspended at a far-field distance $F = 233.75$ mm from the center point of the (6, 6) element with an incident angle of $\theta_i = 20^\circ$. Design procedure of the proposed unit element is briefly described here. With reference to Fig. 7, wave propagating from the horn to the (6, 1) element is represented using path P_0 and its reflection phase is ϕ_0 , which is taken to be a reference point. If the path length for another arbitrary element, say (6, 11) element, is labelled as P_n , then the path difference between this particular element and the reference can be denoted as $\Delta P_{n0} = P_n - P_0$. The phase difference is calculated as $\phi_{n0} = \Delta P_{n0} 2\pi/\lambda$. To make the re-radiated wave from the (6, 6) element co-phased with that from the (6, 1) element, the (6, 6) element is compensated with a phase ϕ_{n0} , which can be found from the y -axis of Fig. 3, such that making it a constant at a certain phase $\phi_n = \phi_0 + \phi_{n0}$. From the same figure, also, ϕ_0 is mapped to a geometrical dimension L_1 on the x -axis. The total dimension D of the proposed

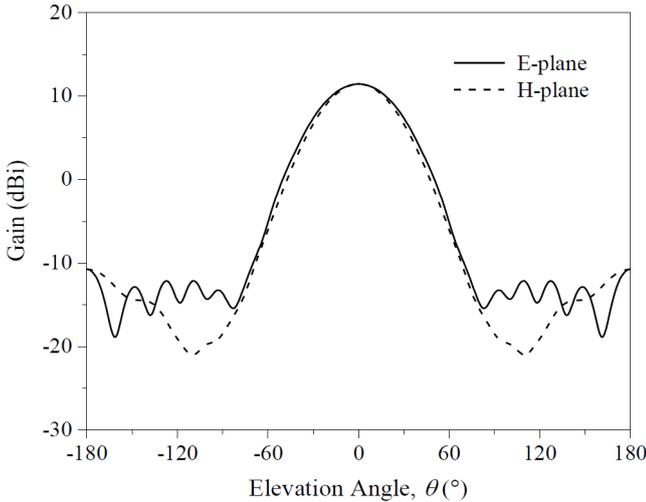


Fig. 6. Simulated radiation patterns of the C-band pyramidal horn.

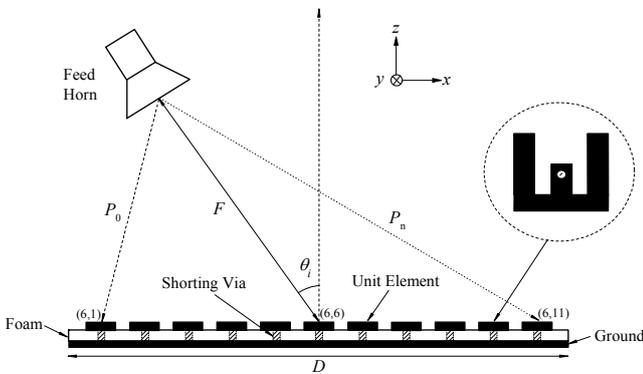


Fig. 7. Configuration of the proposed linearly polarized reflectarray.

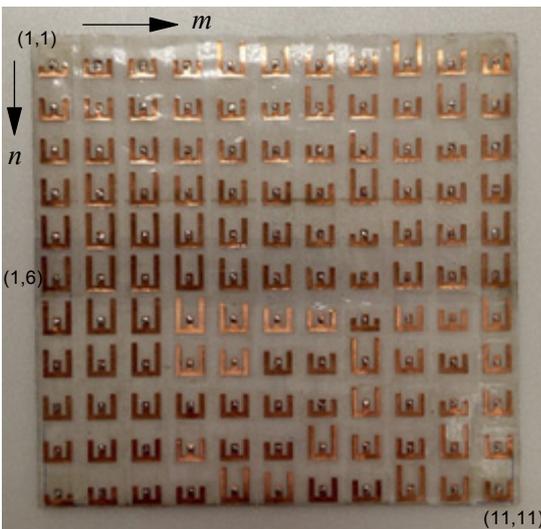


Fig. 8. Photograph of the fabricated prototype of the linearly polarized E-patch reflectarray.

11×11 (121 elements) LP reflectarray is 275 mm, and it has F/D ratio of 0.85. When fabricating the prototype of the proposed reflectarray, the adhesive side of the copper tape was stuck on the surface of a thin transparent paper. Next, the transparent paper with copper layer was lami-

nated with dry film (photopolymer) and exposed to fluorescent light. It was then soaked in etching solution to remove all the unwanted parts of the copper layer. Then, the transparent paper with E-patches was stuck on a square polystyrene foam board, which was backed ground plane. Each of the patches was connected to its ground through a shorting via. It should be mentioned that the thickness and dielectric constant of the transparent paper were not included in simulation. The photograph of the fabricated prototype of the proposed E-patch reflectarray is shown in Fig. 8.

4. Measurement Setup

Measurement is conducted in free space environment for measuring the radiation patterns and antenna gain of the proposed reflectarray. Figure 9 shows the measurement setup. The reflectarray under test is placed on a rotating table and it is connected to a signal generator (Rohde & Schwarz SMB100A) for supplying a transmitting microwave signal with power (P_i) of 10 dBm at the desired frequency. Then, a linearly polarized C-band pyramidal horn (ATM PNR137-440-2, 5.85 GHz–8.2 GHz) is placed at a far-field distance $R = 8.5$ m from the reflectarray and it is used to receive power (P_r) from the reflectarray. The receiving horn is connected to an Advantest U3771 spectrum analyzer for reading the receiving power. To enable measurement of radiation patterns in all angles, the reflectarray is directed facing $+z$, and it is rotated in the θ direction. At each elevation angle, the received power is directly recorded from the spectrum analyzer. The antenna gain can then be calculated using Friis Transmission equation.

5. Results and Discussion

Figure 10 shows the simulated and measured radiation patterns of the proposed E-patch reflectarray in the E (yz -plane) and H (xz -plane) planes. Good agreement is observed between the simulated and measured curves. A simulated peak gain of 24.56 dBi is observed in the boresight direction ($\theta = 0^\circ$) in both planes. With reference to the same figure, the measured peak gains for E and H planes are found to be ~ 23.7 dBi, which corresponds to an aperture efficiency of 36% (simulation 43.4%). The discrepancies can be caused by fabrication tolerances as it is very challenging to solder the vias accurately. The simulated co-polarized fields are at least 20 dB larger than their cross-polarized counterparts in the boresight direction ($\theta = 0^\circ$). On the other hand, the measured co-polarized fields are found to be only ~ 18 dB larger than their cross-polarized components in the boresight, which can be caused by imperfections in experiment. Figure 11 shows the simulated and measured antenna gain (at $\theta = 0^\circ$) as a function of frequency. The measured -1 dB gain bandwidth is covering the frequency range of 7.1 GHz–7.7 GHz (simulation 7.4 GHz–8.2 GHz), with a bandwidth of 8.1% (simulation 10.26%). Again, fabrication tolerances can be

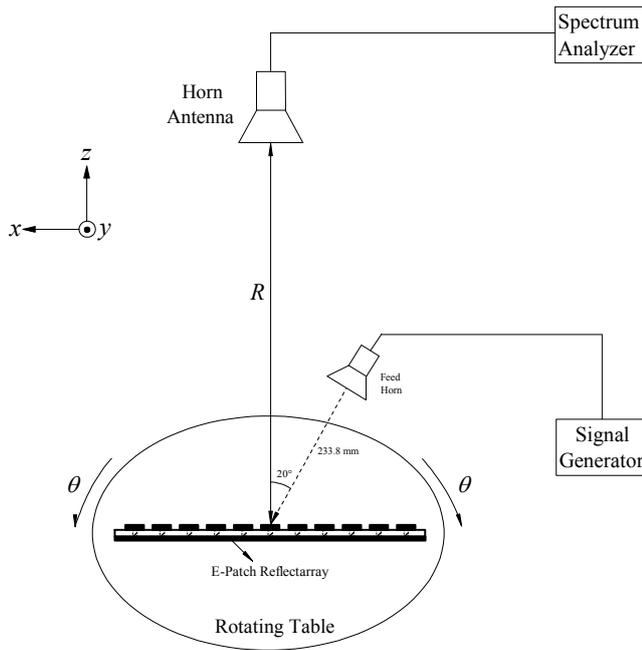


Fig. 9. Measurement setup for the reflectarray.

one of the issues that contribute to the shift. To compare the performances of the reflectarrays that are designed using the E-shaped patch and the rectangular patch, a 9×9 (81 elements) rectangular patch reflectarray is designed and simulated at 7.9 GHz. The array size is limited by the phase range (292°) of the rectangular patch. It is found that a simulated antenna gain of 22.8 dBi is achievable, with a -1 dB gain bandwidth of 7.6 % (7.6 GHz–8.2 GHz). Although the -1 dB bandwidth of the rectangular patch reflectarray is comparable with that of the E-patch reflectarray, its reflection phase range is still much less than 360° . It was reported in [21, 22, and 23] that the single-layered microstrip reflectarrays which are designed using variable sizes of patches can provide a phase range of only $\sim 330^\circ$, which is insufficient for designing a large-sized reflectarray. Unlike the rectangular patch element, the proposed E-shaped patch element is able to achieve a phase range of $\sim 360^\circ$ with the use of only a single layer. Table 1 compares the performances of the proposed reflectarray with some of the linearly polarized reflectarrays in literature. As can be seen from the table, our reflectarray has reasonable gain, bandwidth, and aperture efficiency.

6. Parametric Analysis

Parametric analysis is performed to study the characteristics of the proposed unit element and the LP reflectarray. To begin with, the E-patch without a shorting via is simulated for comparison. Figure 12 shows the simulated reflection phases for the E-patch with and without a shorting via. With reference to Fig. 12, a sharp change in gradient is observed in the phase curve in the range of $L_1 = 6.2$ mm to 6.4 mm when the via is removed, causing it not suitable to be used for reflectarray design. Although the gradient becomes slower beyond $L_1 = 6.4$ mm, the phase

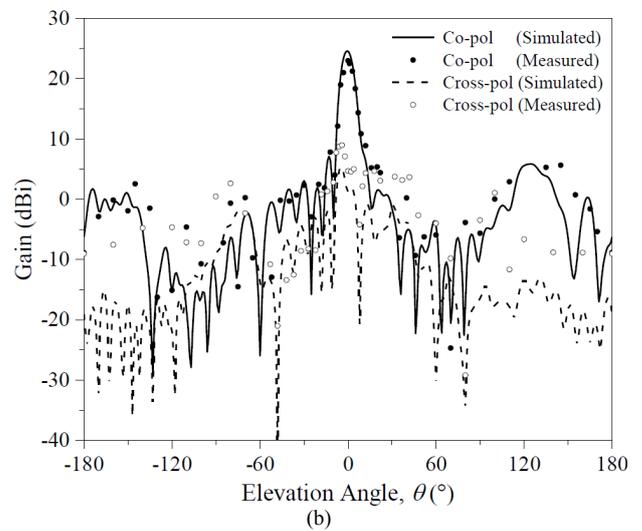
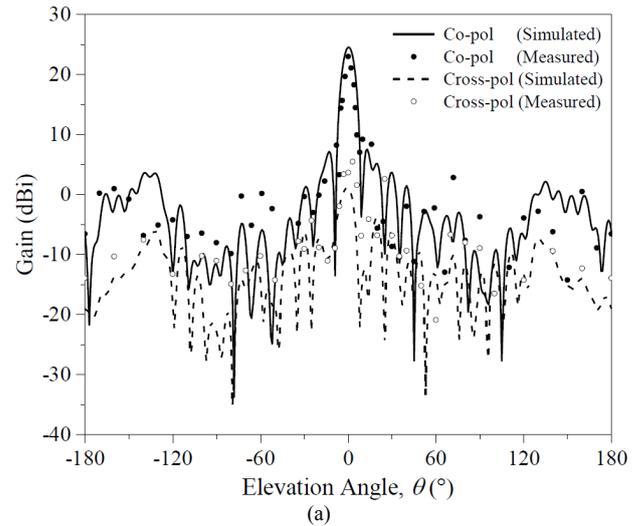


Fig. 10. Measured and simulated (a) E- and (b) H- plane radiation patterns of the proposed E-patch reflectarray.

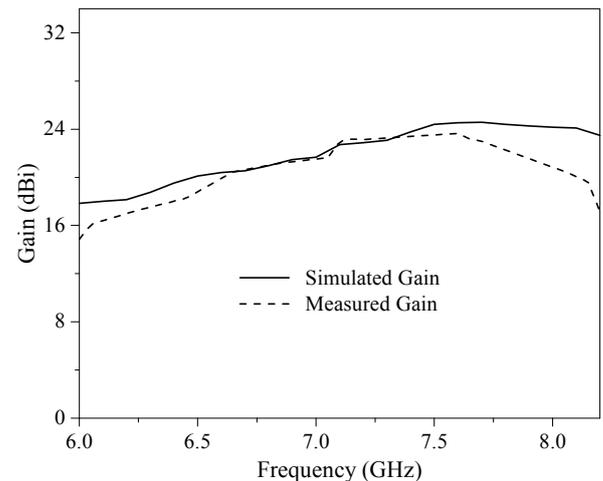


Fig. 11. Measured and simulated antenna gain of the proposed E-patch reflectarray as a function of frequency.

range is less than 360° . Figure 13 shows the surface current distribution of the E-patch without via. It is obvious that the current is concentrating at the center arm of the E-patch

Reference No.	No. of Reflectarray Element	Reflectarray Aperture Size (mm ²)	Gain (dBi)	Gain Bandwidth		Aperture Efficiency (%)
				-1dB (%)	-3dB (%)	
24	27 × 27 = 729	405 × 405	28.5	8	-	34.12 (measured)
6	-	280 × 210	26.2	-	17	37 (measured)
25	29 × 29 = 841	246.5 × 246.5	34	8	-	41 (simulated)
5	21 × 31 = 651	190 × 270	24	-	18	35 (measured)
26	11 × 5 = 55	660 × 300	14.2	-	14.1	22.6 (simulated)
This work	11 × 11 = 121	275 × 275	23.7	8.1	19.8	36 (measured)

Tab. 1. Performances of the linearly polarized reflectarrays.

and there is no current flow to the two arms, resulting in less phase change when the lengths of the two arms are varied. On the other hand, the E-patch with via is able to achieve a phase range of ~360° with slow gradient.

Now, the effects of the arm widths (W_1 and W_3), separation gaps (G_1 and G_2), foam thickness (h), and unit cell size (L) are studied. To start, the two arm widths (W_1 and W_3) are varied and the corresponding reflection phases are shown in Fig. 14. W_1 and W_3 are made to be equal in this case. With reference to Fig. 14, the increase in phase range

is observed when varying the parameters W_1 and W_3 from 1 mm to 5 mm. However, the usable L_1 length for the case of ($W_1 = W_3 = 4$ mm and 5 mm) is still in the range of 5mm to 15mm as the curve gradient becomes too steep beyond $L_1 = 15$ mm. For $W_1 = W_3 = 1$ mm, although the entire range of L_1 can be used, its achievable phase range is lesser than 360°. With reference to Fig. 15, it is observed that the side and back lobes of the reflectarray become larger when the arm widths (W_1 and W_3) are varied from 3 mm to 5 mm. It causes the antenna gain to reduce at $\theta = 0^\circ$, as can be seen in Fig. 15. In our design, the arm widths ($W_1 = W_3 = 3$ mm) are chosen as they enable the reflectarray element to produce a phase range of ~360°, with slow curve gradient and maximum antenna gain.

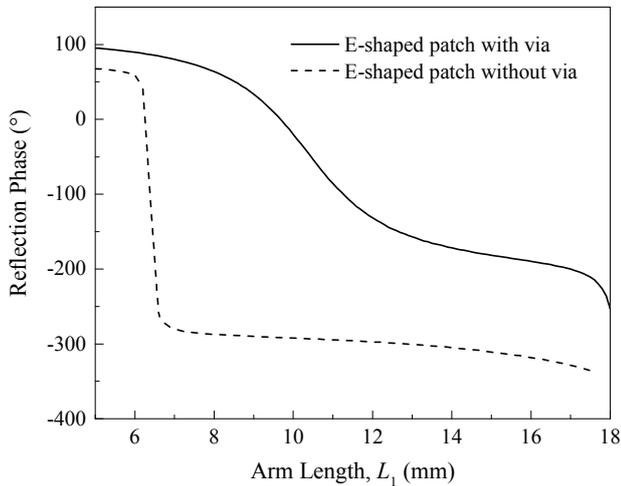


Fig. 12. Reflection phases of the E-patch element with and without shorting via.

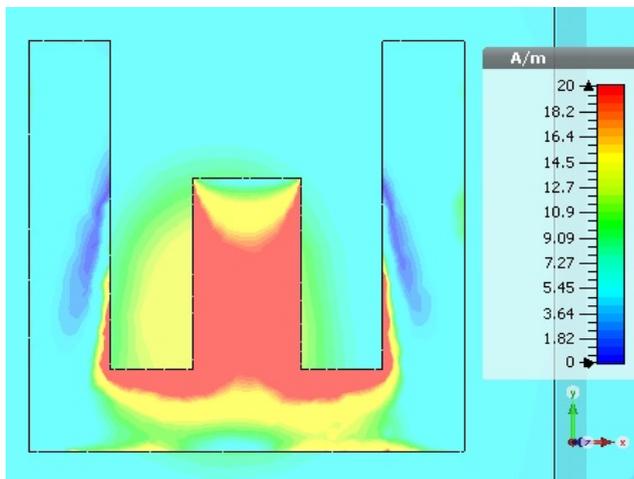


Fig. 13. Surface current on the E-shaped patch without via for the case of $L_1 = 12$ mm.

The effects of the separation gaps (G_1 and G_2) between two adjacent arms are studied and their reflection phase curves are plotted in Fig. 16. In this case, G_1 and G_2 are set to be the same. As can be seen from the curve for ($G_1 = G_2 = 5$ mm and 6 mm), rapid phase change is observed for L_1 beyond 14 mm, introducing sudden increase in the total phase range, although it is too steep to be useful. Similar trend is observed when broadening the gap separations (G_1 and G_2) from 1 mm to 3 mm. For the case of ($G_1 = G_2 = 3$ mm), minor increase is observed in the total phase range. With reference to the radiation patterns in Fig. 17, the side lobes become larger in the H -plane when (G_1 and G_2) are increased from 3 mm to 6 mm. Low side lobes and optimum antenna gain are observed for $G_1 = G_2 = 3$ mm.

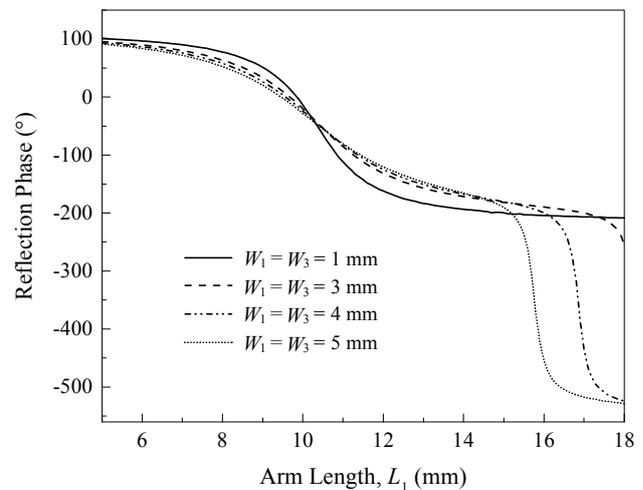


Fig. 14. The effect of arm widths (W_1 and W_3) on the reflection phase of the E-patch reflectarray unit element.

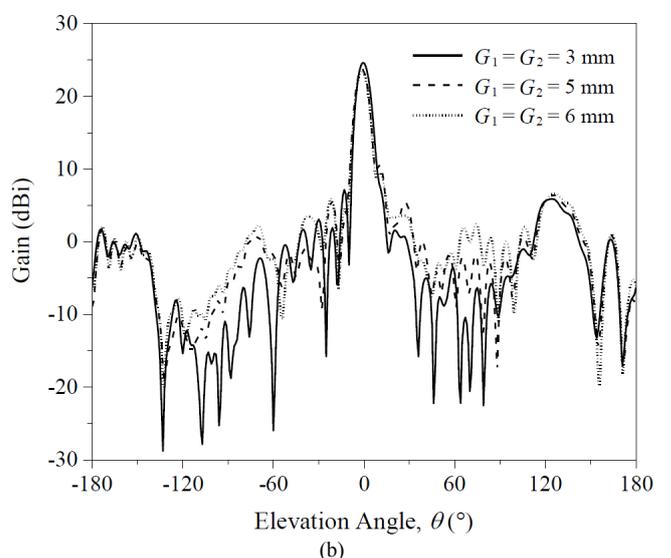
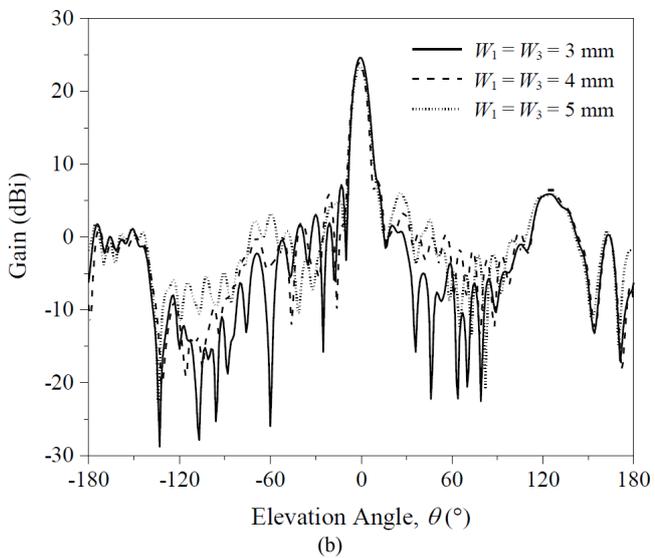
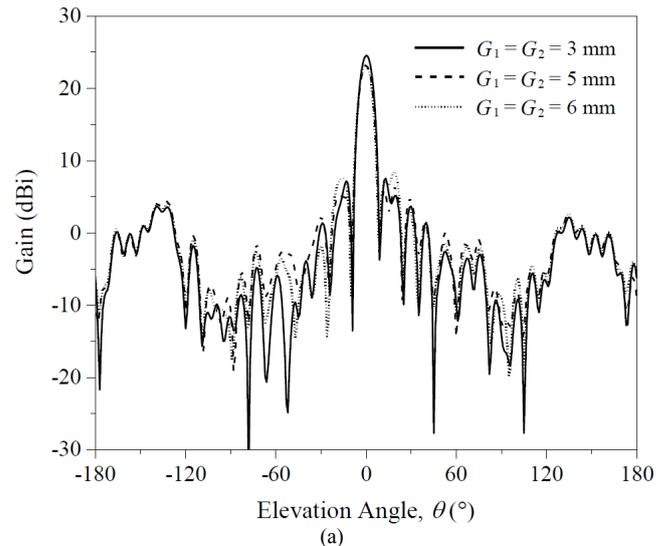
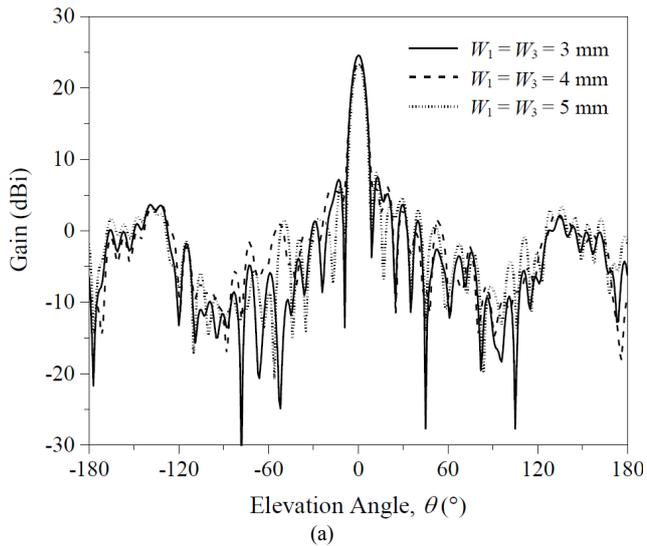


Fig. 15. Radiation patterns of the proposed E-patch reflectarray with different arm widths (W_1 and W_3). (a) E - and (b) H - planes.

Fig. 17. Radiation patterns of the proposed E-patch reflectarray with different gap separations (G_1 and G_2) between two adjacent arms. (a) E - and (b) H - planes.

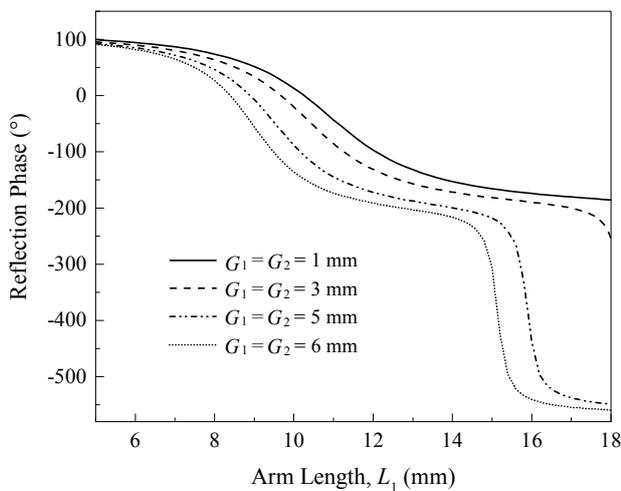


Fig. 16. The effect of gap separations (G_1 and G_2) on the reflection phase of the E-patch reflectarray unit element.

Subsequently, the thickness of the foam (h) is varied and its reflection phase response is shown in Fig. 18. It is observed that the reflection phase range increases when h is increased from 2 mm to 7 mm. For the case of $h = 7$ mm, the gradient of the phase curve becomes very steep when the arm length (L_1) goes beyond 16 mm, and this portion cannot be used for designing reflectarrays limited by our fabrication precision. As a result, the achievable phase range $\sim 260^\circ$ is not sufficient for designing a full-fledge reflectarray. On the other hand, for the case of $h = 2$ mm, the unit element is able to produce a phase range of 327° , which is slightly less than one full cycle (360°).

Next, the effects of the unit cell size (L) on the reflection characteristics are studied. The reflection phase curves for $L = 0.606\lambda$, 0.658λ and 0.711λ are almost overlapping, as can be seen from Fig. 19. The cell size is translated into separation distance between two adjacent elements when the unit element is employed for designing a full-fledge

reflectarray. The radiation patterns for separation distances of 0.606λ , 0.658λ and 0.711λ are depicted in Fig. 20. Antenna gain in the boresight direction is found to be larger with lower backlobe level when the separation distance is increased. This can further improve the front-to-back ratio, which is much desirable. In our design, however, the separation distance is selected to be $L = 0.658\lambda$ as the side lobes are lower for this case.

With the use of $L = 0.658\lambda$ and the reflectarray dimension of $D = 11L = 275$ mm, the radiation patterns of the reflectarray for different F/D ratios are illustrated in Fig. 21. It is obvious that the front-to-back ratio decreases when the F/D ratio is increased from 0.85 to 0.95. This can be caused by spill-over losses when the focal distance is increased. However, the ratio can't be made too small as it has to satisfy the far-field criterion. In our case, it is found that the reflectarray design with $F/D = 0.85$ and focal distance of 233.75 mm has given the best radiation performance.

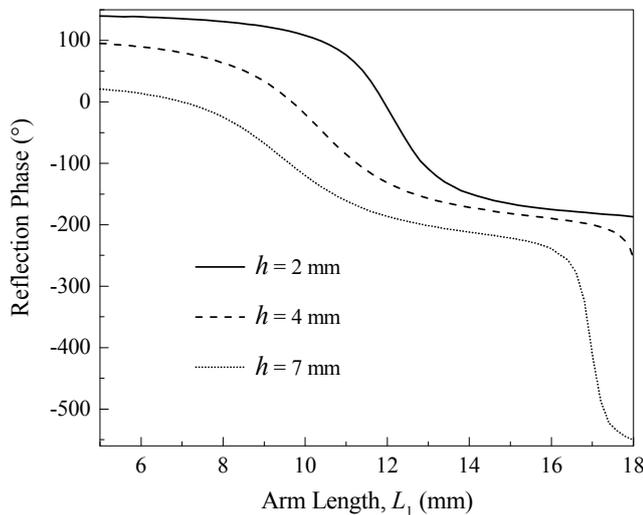


Fig. 18. The effect of foam thickness (h) on the reflection phase of the E-patch reflectarray unit element.

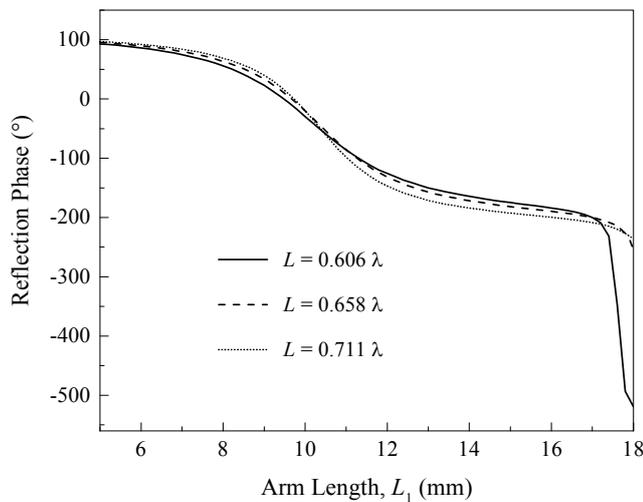


Fig. 19. The effect of the unit cell size (L) on the reflection phase response of the proposed unit element.

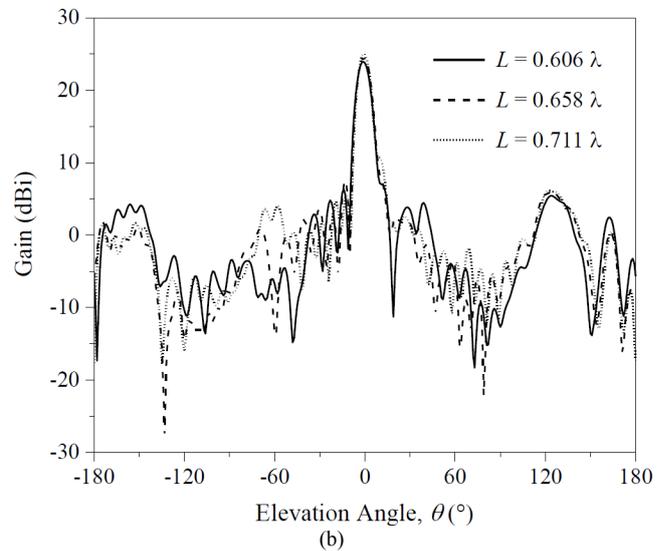
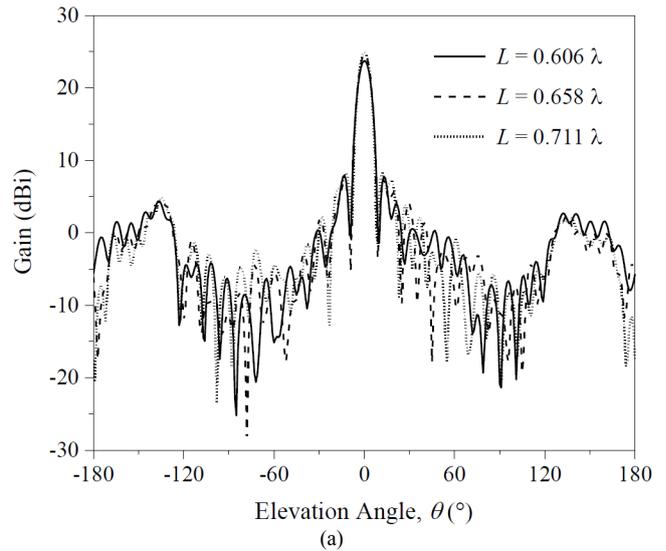


Fig. 20. Radiation patterns of the proposed E-patch reflectarray with different unit cell sizes. (a) E- and (b) H- planes.

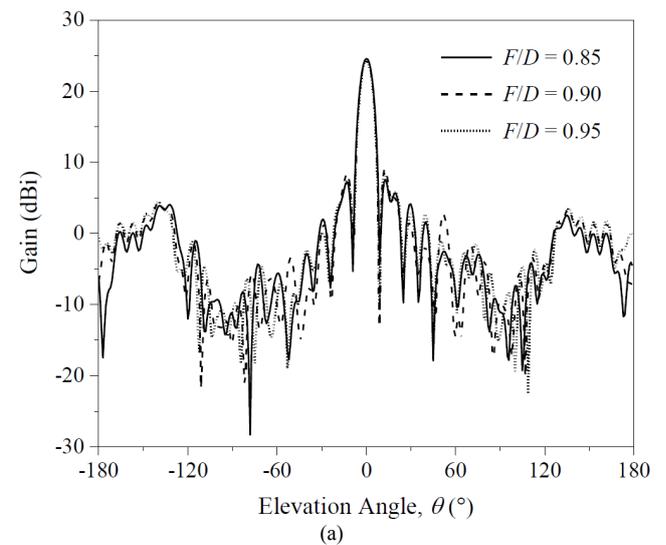


Fig. 21. (a) Radiation patterns of the proposed E-patch reflectarray with different F/D ratios: E- planes.

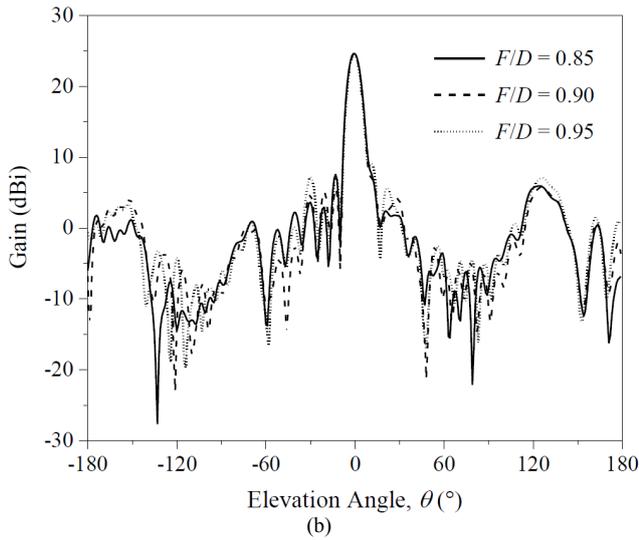


Fig. 21. (b) Radiation patterns of the proposed E-patch reflectarray with different F/D ratios: H - planes.

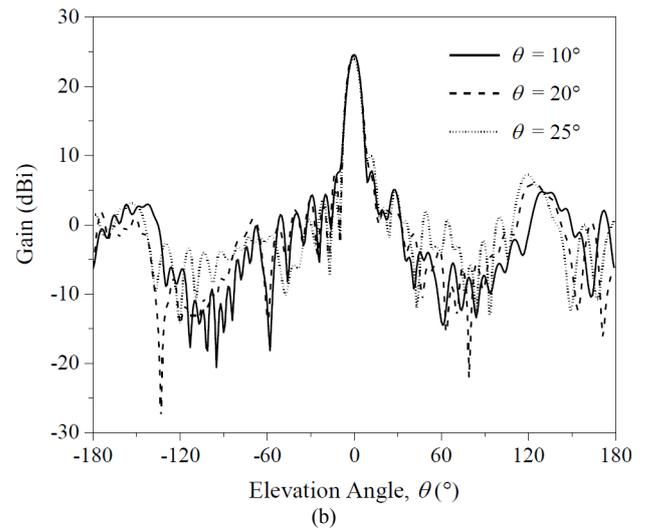


Fig. 23. (b) Radiation patterns of the proposed E-patch reflectarray for different feeding angles (θ): H - planes.

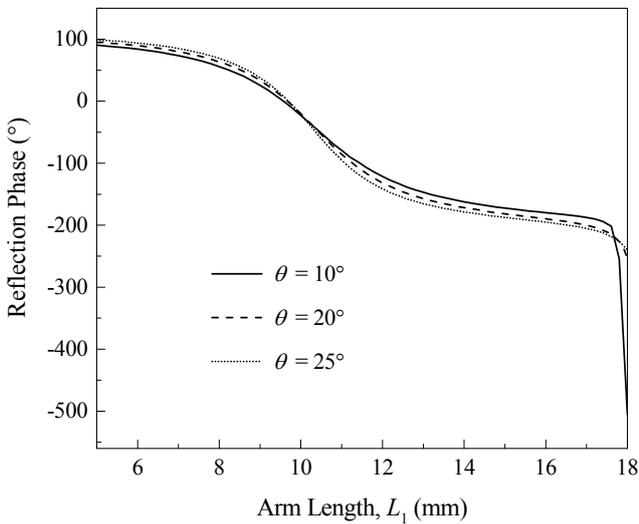


Fig. 22. The effect of feeding angle (θ) on the reflection phase of the E-patch unit element.

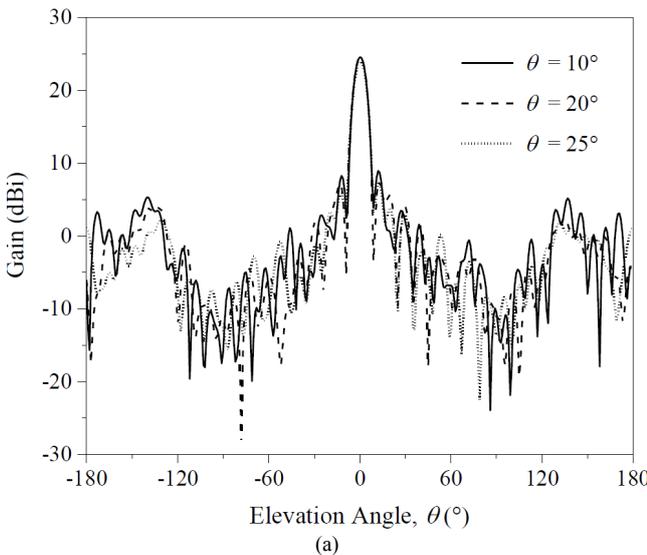


Fig. 23. (a) Radiation patterns of the proposed E-patch reflectarray for different feeding angles (θ): E - planes.

Finally, the feeding angle (θ) is studied. It can be observed from the unit cell simulation that the reflection phase does not vary much when the proposed unit element is fed with an incident angle of 10° , 20° and 25° , as shown in Fig. 22. But it has much effect on the radiation patterns. With reference to Fig. 23, it is noticed that the side and back lobes of the reflectarray become larger when the feeding angle is increased from 10° to 25° . To reduce the effect of feeder blockage, the feeding angle of 20° is selected for our design.

7. Conclusion

A single-layer E-patch reflectarray has been proposed for broadband applications. The unit element has extremely small reflection loss and a phase range of $\sim 360^\circ$. With the use of this element, a full reflectarray has been designed and fabricated. Measurement shows an antenna gain of ~ 23.7 dBi and a -1 dB gain bandwidth of 8.1%. Parametric analysis has been conducted and it was found that the radiation performance of the full reflectarray can be further optimized by manipulating some of the design parameters such as foam thickness, arm length, F/D ratio, and incident angle. The proposed reflectarray is very simple as it does not require the use of any dielectric substrate. It can provide sufficient phase range using one layer. Also, the antenna is lightweight and it can be manufactured with minimum cost.

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