Low-complexity Noncoherent Iterative CPM Demodulator for FH Communication

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Abstract. In this paper, we investigate the noncoherent iterative demodulation of coded continuous phase modulation (CPM) in frequency hopped (FH) systems. In this field, one important problem is that the complexity of the optimal demodulator is prohibitive unless the number of symbols per hop duration is very small. To solve this problem, we propose a novel demodulator, which reduces the complexity by applying phase quantization and exploiting the phase rotational invariance property of CPM signals. As shown by computational complexity analysis and numerical results, the proposed demodulator approaches the performance of the optimal demodulator, and provides considerable performance improvement over the existing solutions with the same computational complexity.

Keywords
Continuous phase modulation, frequency hopping, noncoherent demodulation, iterative demodulation, low-complexity.

1. Introduction

Frequency hopping (FH) is a widely used technique in wireless communication systems, e.g., military anti-jamming communication system and cognitive radio system. One characteristic of FH system is the phase discontinuity between adjacent hop intervals. Consequently, compared with coherent demodulation that requires additional overhead for channel estimation, noncoherent demodulation is more preferred in practical systems, since it does not require explicit knowledge or estimation of channel phase. Moreover, next generation FH communication requires a spectrum efficient transmission waveform that allows the use of low-cost power-efficient amplifiers. In this context, continuous phase modulation (CPM) [1] serves as a good candidate due to its high spectral efficiency and constant envelope property.

In this paper, we investigate the noncoherent iterative demodulation of coded CPM in FH systems. In this field, one important problem is that the complexity of the optimal demodulator is exponential to the hop length (i.e., the number of symbols per hop duration) and thus become prohibitive even for moderate hop length [2]. In order to reduce the complexity, several suboptimal demodulators have been proposed in previous literatures. In [2], a suboptimal demodulator is proposed based on multiple symbol differential detection (MSDD) [3], which evaluates soft symbol decisions over an observation window. However, the performance of the demodulator suffers significant losses as the window size is much smaller than the hop length, at the same time its complexity increases exponentially with the window size. Another suboptimal demodulator [4], [5] is proposed based on the iterative tree search (ITS) and employs M-algorithm [6] to limit the number of paths through the tree. However, the performance of the demodulator suffers significant losses due to two reasons, i.e., only part of the symbols over the hop duration is used to evaluate the soft symbol decisions and the correct path through the tree may be discarded by M-algorithm.

In this paper, a novel noncoherent iterative CPM demodulator for FH communication is proposed. We reduce the complexity by the following three steps. First, we introduce phase quantization [7] into noncoherent demodulation of CPM. In such way, the complexity of noncoherent demodulation is reduced to a level that is comparable to coherent receivers. Second, the phase invariance property of CPM signals [8] is exploited to further reduce the complexity of the proposed demodulator. Furthermore, the phase branch pruning approach [7] is integrated into the proposed demodulator to offer a good trade-off between the complexity and performance. We analyze the computational complexity of our proposed demodulator and evaluate its performance by numerical simulations. It is shown that the proposed demodulator approaches the performance of the optimal noncoherent demodulator, while its complexity grows linearly with the hop length. Moreover, compared with the demodulators presented in [2] and [4], [5], the proposed scheme achieves considerable performance improvement with the same computational complexity.

The rest of the paper is organized as follows. The system model is described in Section 2. The proposed low-complexity demodulator is derived in Section 3. Computational complexity analysis and numerical results are pre-
presented in Section 4 and Section 5, respectively. Finally, conclusions are drawn in Section 6.

2. System Model

2.1 Signal Model

The M-ary CPM signal in the interval \( nT_s \leq t \leq (n+1)T_s \) is described as

\[
s(t; a, \varphi_0, a_{-L+1}, \ldots, a_{-1}) = \sqrt{\frac{2E_s}{T_s}} \exp[j\varphi(t; a, \varphi_0, a_{-L+1}, \ldots, a_{-1})]
\]

with

\[
\varphi(t; a, \varphi_0, a_{-L+1}, \ldots, a_{-1}) = \varphi_0 + 2\pi h \sum_{i=n-L+1}^{n} a_i (t - iT_s)
\]

and

\[
\varphi_0 = (\varphi_0 + \pi h \sum_{i=-L+1}^{-1} a_i) \mod 2\pi
\]

where \( E_s \) is the symbol energy, \( T_s \) is the symbol interval, and \( a \) is the input symbol sequence with \( i \)-th symbol \( a_i \in \{ \pm 1, \pm 3, \ldots, \pm M - 1 \} \). \( h = Q/P \) is the modulation index, where \( Q \) and \( P \) are relative prime integer. The phase pulse \( q(t) \) is the time-integral of a frequency pulse with length \( LT_s \) and area \( 1/2 \), where \( L \) is the length of phase pulse. Moreover, \( \varphi_0 \in \{ 2\pi/P, 4\pi/P, \ldots, 2\pi (P - 1)/P \} \) and \( a_{-L+1}, \ldots, a_{-1} \in \{ \pm 1, \pm 3, \ldots, \pm M - 1 \} \) denote the initial parameters for the CPM modulator.

According to the well known Rimoldi decomposition [9], the CPM modulator can be represented as a cascade of a continuous phase encoder (CPE) and a memoryless modulator. The CPE, in general, is a time-invariant convolutional encoder operating on a ring of integers modulo \( P \). Therefore, by adding an outer convolutional encoder connected to the CPE through an interleaver, a serial concatenated convolutional encoder system [10], [11] is formed. Subsequently, iterative demodulation and decoding can be performed based on maximum a posteriori detection at the receiver.

2.2 Channel Model

Usually, at the baseband, the FH channel is modeled as an additive white Gaussian noise (AWGN) channel where the phase offset is assumed to remain constant over each hop and independent from one hop to the next [2]. After de-hopped and filtered, the baseband received signal of the \( k \)-th hop is described as

\[
r_k(t) = s_k(t; a_k, \varphi_0, a_{-L+1,k}, \ldots, a_{-1,k}) \exp(j\theta_k) + w(t)
\]

over the interval \( iT_s \leq t \leq (i+1)T_s \). Here, \( k = [i/N] \), and the function \( [x] \) rounds \( x \) down to an integer value. \( N \) is the number of symbols per hop and defined as hop length. The symbols of the \( k \)-th hop, \( \{ a_{0N}, a_{N+1}, \ldots, a_{N+N-1} \} \) are denoted as \( a_k = \{ a_{0,k}, a_{1,k}, \ldots, a_{N-1,k} \} \), and the last \( L - 1 \) symbols of the \( (k - 1) \)-th hop, \( \{ a_{0N}, a_{1N}, \ldots, a_{N-1} \} \), are denoted as \( a_{-L+1,k}, \ldots, a_{-1,k} \). The initial phase of the \( k \)-th hop, \( \varphi_{0,k} \), is denoted as \( \varphi_{0,k} \). Moreover, \( w(t) \) denotes the additive white Gaussian noise with power spectral density \( N_0 \) W/Hz, and \( \theta_k \) represents the phase offset for the \( k \)-th hop. \( \theta_k \) is uniformly distributed over the range \( [0, 2\pi) \), and is modeled as independent from one hop to the next.

2.3 System Description

Fig. 1 shows a schematic block diagram of the overall system. The channel encoder encodes a sequence of information bits \( b \) into a sequence of coded bits \( c \). The resulting coded sequence is interleaved by a random permutation and is then mapped to a sequence of \( M \)-ary symbols. The \( M \)-ary sequence is then passed to the CPM modulator, which acts as an inner recursive encoder. Subsequently, a frequency hopper hops the carrier over different frequencies.

At the receiver end, a frequency de-hopper drives the CPM signal back to base band. Subsequently, for each hop of received samples, the hop-wise demodulator computes a posteriori probabilities (APPs) \( P_s^h \). The extrinsic part of these bit-wise APPs \( z^h \) are then de-interleaved and passed to the channel decoder. The
channel decoder performs one decoding iteration and
_generates the bit-wise extrinsic information $\eta^b_e$. Then the
 interleaved bit-wise extrinsic information $\lambda^b$ are fed back to
the demodulator, which update the prior symbol probabilities $\lambda^e$. After a fixed
number of iterations, decisions are made at the output of the channel decoder to
generate the decoded bits $b$.

3. Proposed Low-complexity Noncoherent Iterative CPM Demodulator for FH Communication

As we have mentioned, the noncoherent iterative
demodulator operates hop-wise. Therefore, without loss
of generality, we drop the subscript $k$ for simplicity in the
following. Notice that $a_{L-1}, \ldots, a_1$ are the last $L-1$ symbols of the previous hop. Here, we use the temporary hard decisions of $a_{L-1}, \ldots, a_1$ as the their values. Without loss
of generality, we assume that $a_{L-1} = \cdots = a_1 = 1$ and
hide the condition $a_{L-1} = \cdots = a_1 = 1$ for simplification. Consequently, (4) turns out to be

\[ r(t) = s(t; a, \phi_0) \exp(j\theta) + w(t) \] (5)

Here, we introduce some notations that we will use throughout this paper. We restrict our attentions to the case
where $M$ is a power of two, and define $m = \log_2 M$ as the number of bits in each CPM symbol. Denote the input vector
for the CPM modulator by $a = \{a_0, \ldots, a_{N-1}\}$. For each
$i = 0, \ldots, N-1$, $a_i \in \{\pm 1, \pm 3, \ldots, \pm M - 1\}$ represents
an input CPM symbol encoding $m$ bits. The bits encoded in $a_i$ are denoted by $\{a^i_l, j = 1, \ldots, m\}$.

For each bit $a^i_l$, $0 \leq l \leq N-1, 1 \leq j \leq m$, let $\lambda^b_{a^i_l}(w) = Pr[a^i_l = w], w = 0, 1$ denote the input bit-wise priors provided by the
channel decoder. We assume that these bit-wise priors associated with the same block are independent due to
the presence of channel interleaver. Based on this independency assumption, the demodulator takes the following three
steps to compute the output bit-wise extrinsic information to be passed back to the channel decoder.

1) For each symbol $a_i$, the demodulator generates
symbol-wise priors $\lambda^e_i(a_i)$ from input bit-wise priors $\lambda^b_{a^i_l}(a^i_l)$ as

\[ \lambda^e_i(a_i) = \prod_{l=1}^{m} \lambda^b_{a^i_l}(a^i_l). \] (6)

2) For each symbol $a_i$, the demodulator computes
symbol-wise APPs $\zeta^b_i(u) = Pr(a_i = u), u = \pm 1, \pm 3, \ldots, \pm M - 1$ as

\[ \zeta^b_i(u) = \sum_{a_i \in \Phi} \sum_{a_{i+1} \in \Phi} Pr(s(t; a, \phi_0) | r(t)) \]
\[ \approx \sum_{a_i \in \Phi} \sum_{a_{i+1} \in \Phi} Pr(r(t) | s(t; a, \phi_0)) Pr(a) Pr(\phi_0) \]
\[ = \sum_{a_i \in \Phi} \sum_{a_{i+1} \in \Phi} Pr(r(t) | s(t; a, \phi_0)) \prod_{l=1}^{M} \lambda^b_{a^i_l}(a_i) Pr(\phi_0) \] (7)

where $\Phi = \{2\pi/P, 4\pi/P, \ldots, 2\pi(P-1)/P\}$.

Moreover, the temporary hard decisions of $a_i, i = N-L+1, \ldots, N-1$, to be used in the demodulation of the next
hop, are obtained by $a_i = \arg \max_u [\zeta^b_i(u)]$.

3) For each bit $a^i_l$, the demodulator generates updated
bit-wise APPs $\zeta^b_{a^i_l}(w), w = 0, 1$ and bit-wise extrinsic information $\zeta^b_{a^i_l}(w), w = 0, 1$. The latter is then passed back to
the channel decoder.

Using the symbol-wise APPs, we have

\[ \zeta^b_{a^i_l}(w) = \sum_{a_i \in \Phi} \zeta^b_i(a_i), w = 0, 1. \] (8)

Then the bit wise extrinsic information $\zeta^b_{a^i_l}(w)$ is obtained by removing bit-wise priors $\lambda^b_{a^i_l}(w)$ from $\zeta^b_{a^i_l}(w)$, i.e.,

\[ \zeta^b_{a^i_l}(w) = \frac{\zeta^b_{a^i_l}(w)}{\lambda^b_{a^i_l}(w)}, \zeta^b_{a^i_l}(1-w) = \frac{\zeta^b_{a^i_l}(1-w)}{\lambda^b_{a^i_l}(w)} \] (9)

3.1 Optimal Noncoherent Iterative CPM Demodulator for FH Communication

From (6)-(9), it can be seen that computing $Pr[r(t) | s(t; a, \phi_0)]$ turns out to be the bottleneck in terms of computational efficiency. For optimal noncoherent demodulation, $Pr[r(t) | s(t; a, \phi_0)]$ is described as [2]

\[ Pr[r(t) | s(t; a, \phi_0)] \approx I_0 \left[ \frac{2}{N_0} \int_0^{NT} \exp(r(t) s(t; a, \phi_0)) dt \right] \] (10)

where $I_0(\bullet)$ represents the modified zero order Bessel function of the first kind.

As is seen, the number of the terms in the summation of (7) is equal to $M^N$, which increases exponentially with the hop length. In contrast to the coherent setting where $\theta$ is known, the noncoherent conditional density $Pr[r(t) | s(t; a, \phi_0)]$ shown in (10) cannot be computed recursively, because it does not decompose into a product of suitable individual terms. Therefore, when (10) is used to compute symbol APPs, the resulting complexity is prohibitive, even for moderate hop length.

3.2 Proposed Low-complexity Demodulator Based on Phase Quantization

In this subsection, we introduce a phase quantization
approach, which was previously used in the noncoherent
demodulation of quadrature amplitude modulation (QAM) in
[7], into the demodulation of CPM signals. The main idea of
this approach is to approximate the noncoherent channel by
a set of coherent channels. It is achieved by discretizing the
unknown channel with the phase shift $\theta$. 

First, we assume that $\theta$ takes only $K$ discrete values in the interval $[0, 2\pi/K]$, i.e.,

$$\theta \in \{0, \frac{1}{K}2\pi, \ldots, \frac{K-1}{K}2\pi\}. \quad (11)$$

Next, we approximate $\Pr[r(t) \mid s(t; a, \varphi_0)]$ as

$$\Pr[r(t) \mid s(t; a, \varphi_0)] \approx \frac{1}{K} \sum_{k=0}^{K-1} \Pr[\theta = 2\pi k/K, r(t) \mid s(t; a, \varphi_0)] = \frac{1}{K} \sum_{k=0}^{K-1} \Pr[\theta = 2\pi k/K] = \frac{1}{K} \sum_{k=0}^{K-1} \Pr[\theta = 2\pi k/K]. \quad (12)$$

Finally, we substitute (12) into (7) to approximate $\Pr[r(t) \mid s(t; a, \varphi_0)]$ and get the result shown in (13) at the top of the page.

Based on (13), we can compute $\zeta'_i(u)$ recursively using the BCJR algorithm [12]. The overall computation requirement is equivalent to $K$ times the complexity of a BCJR algorithm applied to the coherent demodulation.

### 3.3 Complexity Reduction by Exploiting the Phase Rotational Invariance Property of CPM Signals

In this subsection, further complexity reduction is achieved by exploiting the phase rotational invariance property of CPM signals for the proposed demodulator. This approach involves following three steps.

1) It has been known that CPM is rotational invariant to $P - 1$ phase ambiguities including $\{2\pi/P, 4\pi/P, \ldots, 2\pi(P - 1)/P\}$ [8], i.e.,

$$s(t; a, \varphi_0)e^{j2\pi\varphi/p} \mid \varphi = 0 = s(t; a, \varphi_0) \mid \varphi = \varphi + 2\pi/p. \quad (14)$$

where $\phi \in \{0, 2\pi/P, \ldots, 2\pi(P - 1)/P\}$ and $v = 0, 1, \ldots, (P - 1)$.

2) According to (1)-(3), $s(t; a, \varphi_0)$ can be described as

$$s(t; a, \varphi_0) = \Gamma(t; a) \exp(j\varphi_0) \quad (15)$$

where $\Gamma(t; a) = s(t; a, \varphi_0) \exp(-j\varphi_0)$ is a function unrelated to $\varphi_0$. Substituting (10) and (15) into (7), we have

$$\zeta'_i(u) \approx \sum_{a, \varphi = u} \frac{2^N}{N_0} \int_0^{\pi} \Gamma(t; a) \exp(j\varphi) dt \prod_{i=1}^{N} \lambda'_i(a_i). \quad (16)$$

According to (16), the output APPs do not depend on the value of $\varphi_0$ for noncoherent demodulation. Therefore, without loss of generality, we assume that $\varphi_0$ takes any value in $\{0, 2\pi/P, \ldots, 2\pi(P - 1)/P\}$ with equal probability. As a result, we have

$$\Pr(\varphi_0 = 0) = \cdots = \Pr(\varphi_0 = 2\pi(P - 1)/P) = 1/P. \quad (17)$$

3) We show that, when the quantization level $K$ is an integer multiple of $P$, (13) can be simplified. Instead of quantizing the phase shift $\theta$ in the interval $[0, 2\pi]$, we quantize it in the subinterval $[0, 2\pi/P]$, thus reducing the number of quantization levels. The reduced phase quantization level $K'$ is equal to $K/P$. Writing any number $k$, $0 \leq k < K$ in the form $k = p'K' + k'$, where $0 \leq p' < P$ and $0 \leq k' < K'$, we rewrite (13) as (18), shown at the bottom of the page.

Define $\Phi(p') = \{2\pi p'/P, 4\pi p'/P, \ldots, 2\pi(p' - 1)/P\}$, $p' = 0, 1, \ldots, P - 1$. Substituting (14) and (17) into (18), we obtain the result shown in (19) at the bottom of the page.

Finally, using the fact that $s(t; a, \varphi_0) \mid \varphi = 0 = s(t; a, \varphi_0) \mid \varphi = \varphi + 2\pi/p$, $\phi \in \{0, 2\pi/P, \ldots, 2\pi(P - 1)/P\}$, we obtain the result shown in (20) at the bottom of the page.
max \Pr(a(r(t)|s(t; a, q_0), \theta = 2\pi k' / K) = \max_{a} N \prod_{F \geq 1} \sum_{q_0 \in \Phi t \in 1} 2 \Re \left( \int_{t}^{t^*} e^{-j2n_k / K} \right) N_0 \lambda_k'(a_k), k' = 0, 1, \ldots, K' \right)

\text{(21)}

<table>
<thead>
<tr>
<th>Demodulator</th>
<th>Additions</th>
<th>Multiplications</th>
<th>Comparisons</th>
<th>Nonlinear functions</th>
</tr>
</thead>
<tbody>
<tr>
<td>PQ demodulator, without phase branch pruning</td>
<td>$4K'NS$</td>
<td>$16K'NS$</td>
<td>0</td>
<td>$4K'N$</td>
</tr>
<tr>
<td>PQ demodulator, with phase branch pruning</td>
<td>$4K'N+4GN(S-1)$</td>
<td>$16K'N+16GN(S-1)$</td>
<td>2N</td>
<td>$4K'N$</td>
</tr>
<tr>
<td>MSDD demodulator</td>
<td>$2WNS+(4W-2)2W^N$</td>
<td>$W2WNS+(4W+1)2W^N$</td>
<td>0</td>
<td>$2W^N$</td>
</tr>
<tr>
<td>ITS demodulator</td>
<td>$7BNS$</td>
<td>$9BNS$</td>
<td>$BNS$</td>
<td>$3BNS$</td>
</tr>
</tbody>
</table>

Tab. 1. Approximated computational complexity per hop for the proposed PQ demodulator, the MSDD demodulator and the ITS demodulator with MSK.

From (14) – (20), it is seen that, by exploiting the phase rotational invariance property of CPM signals, the overall computation requirement is further reduced to $K'$ times the complexity of a BCJR algorithm applied to the coherent demodulation.

3.4 Complexity Reduction by Pruning the Phase Branch

The proposed demodulator implemented using coherent demodulation over $K'$ phase bins incurs a $K'$-fold complexity increase relative to coherent systems. Numerical results show, however, that a genie-based system, which uses only the phase bins which are closest to the true channel phase, yield comparable performance to $K'$-fold averaging. We thus investigate a reduced-complexity implementation, which prunes the number of phase branches, especially in later iterations when we have the soft information from the channel decoder. For this purpose, a generalised likelihood ratio test (GLRT) approach, which has been proposed previously in [7], is applied to estimate the phase bins which are closest to the true channel phase.

GLRT operates with the joint probability density function $\Pr(r(t)) s(t; a, q_0), \theta$, and involves following two steps.

1) After first iteration, we maximize the joint likelihood function over the transmitted symbol sequence $a$ on all $K'$ phase bins, respectively, as shown in (21) at the top of the page.

From (21), it is seen that this step can be viewed as the maximum likelihood sequence estimation (MLSE) and thus can be computed with Viterbi algorithm.

2) $G$ phase bins which maximize the function $\Pr(a(r(t)|s(t; a, q_0), \theta = 2\pi k' / K)$ are regarded as the phase bins closest to the true channel phase, where $G$ is a design parameter and $0 < G < K'$. Consequently, after the first iteration, BCJR are computed only on $G$ phase bins instead of $K'$ phase bins with the aid of GLRT. Though this approach will result in performance degradation, it offers a good trade-off between the complexity and performance by varying the value of $G$.

4. Computational Complexity Analysis

For simplification, in what follows, the proposed demodulator, the demodulator presented in [2], and the demodulator presented in [4], [5] are called PQ (phase quantization) demodulator, MSDD demodulator and ITS demodulator, respectively.

In Tab. 1, the computational complexity analysis for the proposed PQ demodulator with minimum shift keying (MSK) is presented, along with those of the MSDD demodulator and the ITS demodulator. As described in the table, $S$, $W$, and $B$ denote the number of iterations, the window size for the MSDD demodulator, and the number of surviving paths limited by M-algorithm for the ITS demodulator, respectively. From the figure, it is seen that the complexity of the MSDD demodulator is exponential to the window size, and consequently, after the first iteration, BCJR are computed only on $G$ phase bins instead of $K'$ phase bins with the aid of GLRT. Though this approach will result in performance degradation, it offers a good trade-off between the complexity and performance by varying the value of $G$. 
while the complexity of the proposed PQ demodulator and the ITS demodulator grows linearly with the hop length.

In order to perform a fair comparison between the demodulators, two cases are considered in which the complexity of the demodulators is at the same level, i.e.,

\[ K' = 8 \], \( G = 4 \) for the ITS demodulator.

Case 2: \( K' = 8 \), \( G = 2 \) for the PQ demodulator.

Furthermore, as shown in Section 5, the proposed demodulator outperforms the other demodulators in both two cases.

5. Numerical Results

In this section, we give the numerical results by Monte Carlo simulations. Here, the performance of the proposed PQ demodulator is investigated in terms of bit error rate (BER) by simulating the system shown in Fig. 1. Moreover, as described in Subsection 2.2, the simulation channel is modeled as the AWGN channel where the phase offset is assumed to remain constant over each hop and independent from one hop to the next. As in [2] and [4], MSK is considered, and rate 1/2 non-recursive convolutional code with generator polynomial [7 5] is used as the channel code. The length of uncoded bit sequence \( b \) is set to be 500, the maximum number of iterations is restricted to 7, and BJCR algorithm [12] is used to decode the convolutional code. The hop length \( N \) is set to be 20 to provide a good tradeoff between bandwidth-efficiency and power-efficiency of waveforms [2], unless stated otherwise.

Figs. 2 and 3 investigate the effects of the parameters \( K', G \), and \( N \) on the performance of the proposed PQ demodulator. From the figures, it is seen that

- As expected, the performance of the proposed PQ demodulator improves as the number of quantization levels \( K' \) increases. However, increasing \( K' \) beyond 8 does not lead to significant performance improvement.

- As \( G \) is 4 and 2, the loss in performance due to phase branch pruning at the BER of \( 10^{-4} \) is approximately 0.15 dB and 0.45 dB, respectively.

- The performance of the proposed PQ demodulator is an increasing function of the hop length \( N \). This result can be explained as follows. According to (20), the probability for each symbol is evaluated over \( N \) symbols in a hop for the proposed PQ demodulator. Therefore, inherently, as \( N \) increases, the performance of the proposed PQ demodulator also improves.

As we have mentioned, the complexity of the optimal noncoherent demodulator is prohibitive even for moderate hop length. Therefore, instead of evaluating the performance of the proposed PQ demodulator by the performance of the optimal noncoherent demodulator, we evaluate it by information-theoretic bounds and the performance of the MSDD demodulator. In Fig. 4, the performance of the proposed PQ demodulator and corresponding information-theoretic bound [13] are presented, along with the performance of coherent demodulator [14] assuming perfect phase offset estimation, the information-theoretic bound of coherent demodulation [15], and the performance of the MSDD demodulator with \( W = 10 \). From the figure, it is seen that

- As \( N = 20 \), the information-theoretic bound of noncoherent demodulation is approximately 0.75 dB from the information-theoretic bound of coherent demodulation. Moreover, for the proposed PQ demodulator, the loss in performance compared to coherent demodulator at the BER of \( 10^{-4} \) is approximately 0.85 dB. This indicates that the performance loss compared to the optimal noncoherent demodulator at the BER of \( 10^{-4} \) is approximately 0.1 dB for the proposed PQ demodulator.

- As \( K' = 8 \), \( W = 10 \), the performances of the proposed PQ demodulator and the MSDD demodulator are comparable. Moreover, increasing \( W \) beyond 10 only leads
to slightly performance improvement [3]. Therefore, we infer that the performance of the proposed PQ demodulator approaches the performance of the optimal noncoherent demodulator.

As we have shown, the performance of the proposed PQ demodulator approaches the performance of the optimal noncoherent demodulator.

For the MSDD demodulator, the probability for each symbol is evaluated over the observation window instead of being evaluated over the hop duration. Consequently, the performance of the demodulator suffers significant losses as window size is much smaller than the hop length.

The performance of the ITS demodulator suffers significant losses due to two reasons, i.e., the demodulator only exploits part of the symbols over the hop duration to estimate the probability for each symbol and the correct path through the tree may be discarded by M-algorithm.

6. Conclusion

In this paper, a low-complexity noncoherent iterative CPM demodulator for FH communication has been proposed. The effectiveness of the proposed demodulator has been verified with comparisons in terms of the computational complexity analysis and BER simulations. It is clearly shown that the performance of the proposed demodulator approaches the performance of the optimal noncoherent demodulator, and is better than the existing solutions when their complexity is at the same level. Moreover, it is shown that the proposed demodulator also offers a good trade-off between the complexity and performance. Therefore, the proposed demodulator provides an important component for FH-CPM system. Furthermore, though the proposed PQ demodulator is proposed for FH system, it can be also used in many other systems where the phase offset can be assumed to remain constant over a block of symbols, e.g., timing division multiple access (TDMA) system, block-interleaved system, etc.

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References


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