Design of Miniaturized
10 dB Wideband Branch Line Coupler
Using Dual Feed and T-Shape Transmission Lines

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Abstract. This paper presents a design mechanism of miniaturized wideband branch line coupler (BLC) with loose coupling of 10 dB. Dual transmission lines are used as a feed network which provides a size reduction of 32% with a fractional bandwidth (FBW) of 60% for 10±0.5 dB coupling but return loss performance is found to be poor in the operating band. For further improvement of return loss performance as well as for size reduction of the BLC, a T-shape transmission lines are used instead of series quarter wavelength transmission lines, and hence the overall size reduction of around 44% with FBW of 50.4% is achieved. The return loss and isolation performance is found to be < 15 dB in the entire operating band (2.5–4.1 GHz) with respect to design frequency 3 GHz. The proposed BLC is analyzed, fabricated and tested.

Keywords
- Branch line coupler, dual line, miniaturization,
- T-shape transmission line (TL), wideband

1. Introduction

Microwave couplers are crucial devices and are used in many microwave subsystems, such as power amplifiers, phase shifter, modulators and power divider and so on [1–4]. In modern microwave circuits there is an increasing demand for wide bandwidth and cost-effective components. Some of the microwave systems require low power to drive sub circuits such as mixers and antenna arrays. Therefore, the ability of couplers to produce arbitrary coupling level is of recent interest.

The branch line coupler (BLC) is the most common among different types of planar couplers, due to its simple design and easy integration with other circuits. The BLC is commonly used for designing tight (3dB) coupler. The major drawbacks of designing a BLC are large circuit size and narrow bandwidth. The circuit area becomes large, as it has a λ/4 series and shunt transmission lines. Researchers have proposed several techniques to reduce the size and the price of the couplers [5], [6]. Various miniaturization techniques such as defected ground structure [7], varying dielectric constant near the side wall [8], left-handed transmission lines [9], lumped element [10] and dual transmission lines in single layered substrate [11] are presented in literatures. However, the trade off in the size reduction is bandwidth, as the miniaturization occurs bandwidth becomes narrower.

Due to the structural dependence of the BLC on the quarter wavelength (λ/4) and characteristics impedances of transmission line, its application is limited to tight coupling and narrow-band circuits. Design of loose coupled BLC requires high impedance line (narrow line width) which is some extent impractical for design of any microwave circuits. Therefore, the designs of loose BLC’s are mere challenges nowadays. Researchers have proposed various design methodology for widening the bandwidth as well as to achieve loose coupling of the BLC’s simultaneously, such as series stub [12], symmetrically coupled port feeding network [13], λ/4 open circuited coupled lines [14], and λ/4 single line transformer as feeding network [15]. In the aforementioned methodologies, extra λ/4 transmission lines are inserted as a feed network to achieve wide bandwidth, as a result of which the size of the coupler is increased by half of a wavelength.

In this manuscript, the design and implementation of a miniaturized wideband loose BLC (10dB) is demonstrated. For designing such BLC extra quarter wave length transmission line have been inserted as a feeding network at all the ports of the conventional BLC. To reduce the coupler size, all λ/4 sections are replaced by dual transmission lines. Therefore size reduction of 32% with FBW of 60% for 10±0.5 dB coupling and return loss performance < 10 dB is achieved. Further miniaturization of the proposed coupler with improved return loss performance is obtained by replacing series λ/4 transmission lines by T-shape transmission lines. As a result the overall size reduction of 44% and return loss performance < 15 dB in the operating band is obtained without affecting coupler performance.
2. Wideband Loose Branch Line Coupler and Its Miniaturization

2.1 Design of Wideband 10dB BLC

The major issue related to conventional BLC is narrow bandwidth due to all \( \lambda/4 \) transmission lines (series and shunt) which resonates at particular frequency. In order to increase the bandwidth of the BLC the extra \( \lambda/4 \) transmission line is used as a feed network. Figure 1 shows the schematic diagram of 10dB BLC with quarter wave length extra feed network. All the sections are of quarter wavelength maintained as per the design values of BLC [15]. The values of the characteristic impedances (\( Z_1, Z_2 \) and \( Z_3 \)) are calculated from the reference [15]. The microstrip widths and lengths corresponding to the characteristic impedances for the Arlon substrate with dielectric constant \( \varepsilon_r = 3.2 \), thickness \( h = 0.787 \) mm and loss tangent of 0.002 is shown in Tab. 1. Figure 2 shows the simulated S-parameters response of the BLC. Figure 2 depicts a 46.7% FBW with coupling level of 10±0.5 dB at the operating frequency of 3 GHz. The return loss is found to be 18.3 dB at the lower (2.3 GHz) and 17.2 dB at the upper (3.8 GHz) edges of the frequency band; similarly at those frequencies the isolation is 17.8 dB and 15 dB, respectively.

2.2 Miniaturization of Wideband 10dB BLC using Dual Transmission Line

As mentioned in the particular section the bandwidth of BLC is increased by introducing extra \( \lambda/4 \) TL as feeding network resulting in the size increment of BLC. By introducing extra element at all ports, the size of the coupler is increased by half of the wave length. In order to reduce the overall size, dual TL is used in place of single \( \lambda/4 \)-long TL at each port. In a dual TL, \( \lambda/4 \) TL of initial design is split into a parallel TL's structure as shown in Fig. 3.

![Fig. 1. BLC with \( \lambda/4 \) feeding network.](image)

![Fig. 2. (a) S-parameters response of BLC. (b) Phase difference (\(<S_{21} - <S_{31}>\)).](image)

![Fig. 3. Equivalent circuit of single TL with dual TL.](image)

Here, \( Z_o, Z_a, Z_b, \theta_a, \) and \( \theta_b \) are defined as the characteristic impedances and the electrical lengths of dual TL’s, respectively, and \( \theta_a < \theta = 90^\circ < \theta_b \). Here \( \theta (90^\circ) \) is the electrical length of the single TL and the transmission matrix (ABCD parameter) is written in (1). Similarly ABCD matrixes are written for both lines 1 and 2 in (2), (3). The expression for the characteristic impedances and the electrical lengths are obtained from relating (1–3) and giving in (4–6). The characteristic impedances (\( Z_a \) and \( Z_b \)) of these dual-lines are calculated from (4–6) by properly selecting the value of their electrical lengths (\( \theta_a \) and \( \theta_b \)). In order to reduce the circuit size, the condition \( \theta_a < \theta = 90^\circ < \theta_b \) and \( \theta_a + \theta_b = 180^\circ \) must be satisfied. Therefore this dual transmission lines are composed of two high impedance lines with high impedance and different electrical lengths. Out of these two lines, longer one (\( \theta_b \)) is meander in shape to reduce the circuit area.

The layout of the proposed BLC and simulated S-parameters response are shown in Fig. 4 and 5 respectively.

![Tab. 1. Dimensions of 10dB reference BLC.](image)
\[
\begin{bmatrix}
A & B \\
C & D
\end{bmatrix} = \begin{bmatrix}
0 & jZ \\
jY & 0
\end{bmatrix},
\]
(1)

\[
\begin{bmatrix}
A_a & B_a \\
C_a & D_a_{\text{line}1}
\end{bmatrix} = \begin{bmatrix}
\cos \theta_a & jZ_o \sin \theta_a \\
jY_a \sin \theta_a & \cos \theta_a
\end{bmatrix},
\]
(2)

\[
\begin{bmatrix}
A_b & B_b \\
C_b & D_b_{\text{line}2}
\end{bmatrix} = \begin{bmatrix}
\cos \theta_b & jZ_o \sin \theta_b \\
jY_a \sin \theta_b & \cos \theta_b
\end{bmatrix},
\]
(3)

\[
Z_a = \frac{Z \cos \theta_b - \cos \theta_a}{\sin \theta_a \cos \theta_b},
\]
(4)

\[
Z_b = -\frac{Z \cos \theta_a - \cos \theta_b}{\sin \theta_a \cos \theta_b},
\]
(5)

\[
\frac{Z_a}{Z_b} = -\tan \theta_b \tan \theta_a.
\]
(6)

Fig. 4. Layout of BLC with dual TL as a feeding network.

From Fig. 5 it is clear that by incorporating the dual transmission line in place of \( \lambda/4 \) TLs as a feed network the return loss \( S_{11} \) performance drastically changes in the operating frequency band. The return loss performance is degraded due to the step changes (cause parasitic effects) at the line joint between the dual TL, series and shunt quarter wavelength line. The \( S_{11} \) performances are found to be 12.2 dB at the lower edge (2.5 GHz) and 10.3 dB at upper edge (4.3 GHz) of the frequency band with isolation of 14.9 dB and 12.54 dB, respectively. To improve the performance and for further reduction of the coupler size, a T-shape TL is used in place of series quarter wavelength line.

### 2.3 Miniaturization and Performance Improvement of Wideband 10dB BLC using T-shape Transmission Line

To improve the performance as well as the size reduction of the BLC, series quarter wavelength TL is replaced by two series lines and one open stub in the middle which looks like a letter ‘T’ as shown in Fig. 6. The ABCD matrix of a series \( \lambda/4 \) TL is given by (1) and open stub is given in (7) where admittance of the stub \( Y = j \tan \theta_d/Z_o \). Furthermore, the ABCD matrix for each of the two TL that has a characteristic impedance of \( \bar{Z}_c \) and electrical length of \( \theta_c \) is given by (8). The overall transmission matrix of a ‘T’ shape TL is equated with \( \lambda/4 \) TL matrix in order to obtain the characteristic impedances and electrical lengths of the proposed T-shape model as shown in (9).

\[
\begin{bmatrix}
A & B \\
C & D_{\lambda}
\end{bmatrix} = \begin{bmatrix}
1 & 0 \\
jY & 1
\end{bmatrix},
\]
(7)

\[
\begin{bmatrix}
A & B \\
C & D_{\lambda}
\end{bmatrix} = \begin{bmatrix}
\cos \theta_c & jZ_c \sin \theta_c \\
jY_c \sin \theta_c & \cos \theta_c
\end{bmatrix},
\]
(8)

\[
\begin{bmatrix}
A & B \\
C & D_{\lambda}
\end{bmatrix} = \begin{bmatrix}
0 & jZ \\
jY & 0
\end{bmatrix} = \begin{bmatrix}
A & B \\
C & D_{\lambda}
\end{bmatrix} \times \begin{bmatrix}
A & B \\
C & D_{\lambda}
\end{bmatrix} \times \begin{bmatrix}
A & B \\
C & D_{\lambda}
\end{bmatrix},
\]
(9)

\[
A = D = 0 = \cos^2 \theta_c - \sin^2 \theta_c - \frac{Z_c \sin \theta_c \cos \theta_c \tan \theta_d}{Z_d},
\]
(10)

\[
B = jZ = jZ_c \sin 2\theta_c - \frac{jZ_c^2 \sin^2 \theta_c \tan \theta_d}{Z_d},
\]
(11)

\[
C = jY = \frac{j\sin 2\theta_c}{Z_c} + \frac{j\cos^2 \theta_c \tan \theta_d}{Z_d},
\]
(12)

\[
Z_c = \frac{Z}{\tan \theta_c},
\]
(13)

\[
Z_d = \frac{Z_c \tan \theta_d \tan 2\theta_c}{2}.
\]
(14)

The ABCD parameters are written in (10–12). Solving (10–11), the characteristic impedances \( Z_c \) and \( Z_d \) of stub loaded T-shape TL in terms of electrical length are obtained as described in (13–14). The values of \( b \) and \( c \) in Fig. 7 are evaluated by properly choosing the electrical lengths \( \theta_c \) and \( \theta_d \) of series line and open stub in order to achieve miniaturization. For this \( \theta_c = 20^\circ \) and \( \theta_d = 40^\circ \) are chosen. Therefore value of \( b \) is obtained from \( \theta_d = 40^\circ \) and the value of \( c \) is obtained from \( Z_d \) by using (14). The layout of the proposed BLC is shown in Fig. 7. The simulated S-parameters responses of the proposed coupler are shown in Fig. 8.
From Fig. 8 it is evident the return loss (S11) performance is improved due to incorporating the T-shape transmission line in place of series \( \frac{\lambda}{4} \)-long TL. The return loss (S11) performance is improved by minimum \(-8\) dB in the whole frequency band. The isolation (S41) performance is improved by \(-7\) dB at the operating frequency.

3. Experimental Results

The proposed 10-dB BLC’s are designed and fabricated at operating frequency of 3 GHz: Design A consists of a dual TL as a feed network and Design B consists of a dual TL along with T-shape TL for miniaturization of wideband BLCs. In design A, electrical lengths of feed network, \( \theta_1 \) and \( \theta_2 \) are chosen as 45° (\( L_1 = L_a \)) and 135° (\( L_b = 4l_1 + 2l_2 + 3l_3 \)) respectively and the corresponding characteristic impedances (\( Z_a \) and \( Z_b \)) are calculated from (4–6), where \( Z \) is 36 \( \Omega \), therefore \( Z_a = Z_b = 102 \) \( \Omega \). Therefore size reduction of 32% is achieved in design A. In design B, the characteristic impedances (\( Z_c \) and \( Z_d \)) and electrical lengths (\( \theta_c \) and \( \theta_d \)) are evaluated from (13–14) where \( Z \) is taken as 24.6 \( \Omega \) and the electrical lengths (\( \theta_c \) and \( \theta_d \)) are selected as 20° and 40°, respectively. Therefore the overall size reduction of around 44% is achieved in design B. The other parameters remain unchanged.

The proposed couplers have been fabricated on Arlon substrate of dielectric constant \( \varepsilon_r = 3.2 \), thickness \( h = 0.787 \) mm and loss tangent of 0.002. The characteristic impedances and optimized design parameters of BLC’s for design A and B are tabulated in Tab. 2. The photographs of the fabricated prototype for both design A and B are shown in Fig. 9.

An Agilent vector network analyzer is used to test the performance of the fabricated BLC’s and compared with the simulated results to ensure that the coupler design exhibits good performance in the real time environment. Figure 10 and 11 show the simulated (Sim) and measured (Mea) S-parameter responses for both designs A and B, respectively. Table 3 illustrates the simulated and measured S-parameters details, FBW and size of proposed couplers (design A and B). FBW is found to be 60% for the coupling level of \( 10 \pm 0.5 \) dB, phase imbalance \( 90° \pm 10° \) and return loss and isolation are \( < -10 \) dB and \( < -15 \) dB for design A, respectively. Similarly for design B, FBW is 50.04% for the coupling (C) level of \( 10 \pm 0.5 \) dB, phase imbalance \( 90° \pm 10° \) with return loss and isolation performance better than around \(-15\) dB.

<table>
<thead>
<tr>
<th>Design A</th>
<th>Impedance (( \Omega ))</th>
<th>Width(mm), length(mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( Z_1 = 36 )</td>
<td>( Z_a = Z_b = 102 )</td>
<td>( W_1 = 0.4, L_1 = 8 )</td>
</tr>
<tr>
<td>( Z_2 = 24.6 )</td>
<td>( W_2 = 4.5, L_2 = 14.6 )</td>
<td></td>
</tr>
<tr>
<td>( Z_3 = 77.76 )</td>
<td>( L_3 = 24 )</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Design B</th>
<th>Impedance (( \Omega ))</th>
<th>Width(mm), length(mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( Z_1 = 36 )</td>
<td>( Z_a = Z_b = 102 )</td>
<td>( W_1 = 0.4, L_1 = 8 )</td>
</tr>
<tr>
<td>( Z_2 = 24.6 )</td>
<td>( a = 9, b = 5.6, c = 4, d = 1.2 )</td>
<td></td>
</tr>
<tr>
<td>( Z_3 = 77.76 )</td>
<td>( L_2 = 16.3 )</td>
<td></td>
</tr>
</tbody>
</table>

Tab. 2. Dimensions of the proposed BLC’s.
Fig. 10. Simulated and measured S-parameters response of design A: (a) S21, S31, S41, (b) S11, (c) S21 and S31 phase.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>(\lambda/4)-long FN</th>
<th>Design A</th>
<th>Design B</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Sim</td>
<td>Sim/Mea</td>
<td>Sim/Mea</td>
</tr>
<tr>
<td>S21</td>
<td>2.4-4.21</td>
<td>2.3-4.1/2.1-4.1</td>
<td>2.41-4.1/2.5-4.1</td>
</tr>
<tr>
<td>S31</td>
<td>2.35-3.75</td>
<td>2.4-4.35/2.2-4</td>
<td>2.4-4/2.4-3.9</td>
</tr>
<tr>
<td>S41</td>
<td>2.14-3.81</td>
<td>2.4-4.0/2.2-3.7</td>
<td>2.4-3.8/2.4-3.7</td>
</tr>
<tr>
<td>S11</td>
<td>1.8-4.31</td>
<td>1.63-4.03/1.7-4</td>
<td>2.1-4.02/2.4</td>
</tr>
<tr>
<td>FBW</td>
<td>46.7%</td>
<td>65%/60%</td>
<td>53%/50.4%</td>
</tr>
<tr>
<td>Area (mm²)</td>
<td>45.9 × 16.1</td>
<td>31 × 16.2</td>
<td>25.5 × 16.2</td>
</tr>
</tbody>
</table>

Tab. 3. Simulated and measured S-parameter performance of the proposed BLCs.

Fig. 11. Simulated and measured S-parameters response of design B: (a) S21, S31, S41, (b) S11, (c) S21 and S31 phase, (d) phase difference (<S21 - <S31).
The proposed design is aimed at miniaturization of the reference (existing) BLC [15] with proposed technique by giving substantially miniaturization of 44%. It is to be further noted that despite the miniaturization, no other performance factors are degraded. Herein lies the advantage of the proposed design over the existing design since the proposed structure is very compact thus making it suitable to be used in compact and sophisticated microwave systems. The wide band property along with other characteristics of the proposed design is also compared with some other works and the comparison is tabulated in Tab. 4. It is found that the BLC in Ref. [14] is larger in size in comparison with that in Ref. [12], [13]. The proposed coupler is smaller in size, which is 52% and 47% smaller compared to the BLC in Ref. [14] and Ref. [12], [13], respectively. Also the FBW of the proposed design is more compared with the Ref. [12–14].

4. Conclusion

A miniaturized wideband BLC is designed using T-shape TL section and dual TL as a feed network in place of λ/4-long series TL. The proposed design provides an overall size reduction of 44% compared to the BLC with single quarter wavelength section as feed network at all the ports. The measured results are completely compiled with the simulated frequency response for 50.4% FBW with isolation and return loss better than 15 dB. The proposed structure is fabricated with standard printed circuit board which is cost effective in terms of mass production, as a result of giving substantially miniaturization of 44%. It is to be further noted that despite the miniaturization, no other performance factors are degraded. Herein lies the advantage of the proposed design over the existing design since the proposed structure is very compact thus making it suitable to be used in compact and sophisticated microwave circuits.

Acknowledgments

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References


| Design | L (GHz) | | | C dB | | FBW (%) | | Area (mm²) |
|--------|--------|--------|--------|--------|--------|--------|--------|
| A      | 3      | 14     | 1.02   | 10.1±0.5 | 22     | 60.4   | 0.50λ<sub>y</sub> +0.25λ<sub>g</sub> |
| B      | 3      | 21     | 0.95   | 10.5±0.5 | 29     | 55.4   | 0.40λ<sub>y</sub> +0.25λ<sub>g</sub> |

Tab. 4. Comparisons of wideband BLC with the proposed one.


[13] WONG, Y. S., ZHENG, S. Y., CHAN, W. S. Multifold bandwidth branch line coupler with filtering characteristic using coupled port...
About the Authors...

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