A Compact Single Layer Reflectarray Antenna Based on Circular Delay-Lines for X-band Applications

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Abstract. This paper presents a compact single layer reflectarray antenna based on a diagonally notched square patch and a pair of circular delay-lines, for X-band applications. The length and width of circular delay-lines are varied and optimized to attain a linear phase range of more than 600°. The effect of incident angle in TE and TM modes at 0°, 15° and 30° is studied, which offers stable angular phase range. The hybrid Finite Element Boundary Integral (FEBI) method is used for simulation of the whole reflectarray system comprising of 27×27 elements and being fabricated on a low cost FR-4 laminate. The measured gain of 24.5 dBi with aperture efficiency of 49.5% is achieved at 10 GHz. The proposed design provides the measured 1-dB gain bandwidth of 12.5% and 3-dB gain bandwidth of 34%. The simulated and measured side-lobe-levels and cross polarizations are less than -25 dB and -40 dB, respectively.

Keywords

Reflectarray antenna, high gain, circular delay-lines, phase range, TE and TM modes, single layer

1. Introduction

Traditional high gain antennas like parabolic reflectors and planar phased-arrays are commonly used in long distance wireless communication links. However, these conventional antennas are not suitable for certain applications due to large curved surfaces, complex feed networks and a non-planar topology [1]. Reflectarray antennas have been evolved recently to substitute and alleviate the limitations of conventional antennas. Reflectarray antenna combines the attractive features of parabolic reflectors and planar phased-array [2]. Reflectarrays are low profile, light-weight, cost effective and have less fabrication complexity, owing to their planar layouts. A reflectarray antenna consists of a flat reflecting surface with a number of phase shifting elements and a ground plane on the flip-side [3]. The parasitic array elements offer an ap-



Fig. 1. Reflectarray antenna configuration.

propriate phase shift to generate a focused beam in the desired direction. Reflectarray antenna is usually illumined by a feed horn antenna placed at a focal distance [4]. Conventional reflectarray antenna configuration is depicted in Fig. 1.

Despite advantages, the major shortcoming associated with a reflectarray antenna is its narrow bandwidth. The bandwidth performance of reflectarrays is mostly limited by two factors; narrow-band behavior of radiating elements and spatial phase delays. A narrow-band response is more significant for small to medium-sized reflectarrays. The bandwidth limitations of reflectarray elements can be improved by several techniques, such as by employing multilayer structures, using thicker substrate and connecting phase delay-lines [5], [6]. A linear phase response and improved bandwidth can be obtained by using these techniques. Single layered reflectarrays with delay-lines are reported more since they are broadband, light weight and have higher fabrication tolerances.

In the existing literature, a number of reflectarray configurations are proposed for high gain, linear phase range and stable angular response. The X-band reflectarray antenna with Minkowski radiating element is reported in [7]. A phase range of more than 360° is achieved by optimizing the width of Minkowski patch. The side-lobe-levels are less than -18 dB with HPBW of 7.4°. A single-layer reflectarray with E-shaped element is reported in [8]. The phase range of 360° is attained by varying the dimensions of

E-shape element. However, the back lobes and side-lobelevels significantly depend on the width and gap between adjacent E-shape arms. Single-layer reflectarray with combination of elements is presented in [9]. It provides broad reflection phase range by changing the length of outer folded-loop. In [10], a square patch element with attached stubs is proposed for broadband reflectarray. This design provides high gain and a stable angular response. The Xband reflectarray using rectangular-shaped patch element is proposed in [11]. However, phase range is 360° only and aperture efficiency of 44% is achieved by changing the grid spacing and element length. A split-ring delay-line configuration is proposed in [12]. The length of delay-line is used to enhance phase range. In [13], a quasi-spiral reflectarray is proposed. The phase range and high gain is achieved by changing the number of spiral turns. The incident angle effect on Transverse Electric (TE), Transverse Magnetic (TM), Feed-to-Diameter (F/D) ratio and phase range is presented in [14]. The microstrip reflectarray with optimized phase range curve is reported in [15]. A gain of 19 dBi is achieved by employing different-sized elements.

In this paper, a compact, single layer, high gain reflectarray is proposed for X-band applications. The proposed design provides broad linear phase range and low cross polarization levels. The X-band reflectarray antenna can be used in aerospace applications, remote sensing and point-to-point communication links. The unit cell comprises of diagonally notched square shape element attached to a pair of circular delay-lines. The proposed design is realized on a low profile FR-4 substrate. A stable angular phase range is observed up to 30° in TE and TM modes. The reflectarray is designed and optimized by using Ansys High Frequency Structure Simulator (HFSS[™]). The simulated and measured results are in good agreement. The rest of the paper is arranged as follows: In Sec. 2, unit cell design and analysis is described. The reflectarray configuration, system simulations and measurements are described in Sec. 3. The paper is finally concluded in Sec. 4.

2. Unit Element Design and Analysis

This section describes the reflectarray unit cell configuration, performance parameters and simulation environment setup.

2.1 Reflectarray Unit Element Configuration

The reflectarray unit element is designed by making a microstrip square patch which resonates at 10 GHz [16]. The square patch inherently has narrow bandwidth and limited phase range. The elements also have large lattice periodicity and low design efficiency. However, compact single layer elements with large linear phase range are desirable. This has been achieved by adding delay-lines to the square patch. Delay-lines provide broad linear phase range and low cross polarization by varying their length and width [1], [5]. Here, as shown in Fig. 2, a single element is obtained by adding pair of delay-line to a square microstrip patch which is diagonally notched on the four corners to enhance the bandwidth.

The reflectarray is created by periodic arrangement of the reflecting parasitic unit elements along with the ground plane on the flip-side of substrate. The proposed design is etched on 1.6 mm thick, low cost FR-4 substrate ($\varepsilon_r = 4.4$, $\tan \delta = 0.02$). The electrical length (θ_s) of delay-lines is varied from 0° to 170° to control the reflection magnitude and phase range of the reflectarray unit element. The lattice periodicity of elements is kept at $0.25\lambda_0$ at 10 GHz frequency. The proposed reflectarray unit element configuration with side view, TE and TM polarization is shown in Fig. 3.



Fig. 2. Design approach of delay-lines based reflectarray.



(c) TE polarization

(d) TM Polarization



Parameters	Value (λ_0)	
$D_{\rm X}$	0.25	
$D_{\rm Y}$	0.25	
$L_{1,}L_{2,}L_{3}$	0.08	
$L_{4,}L_{5}$	0.03	
L_6	0.034	
L_7	.085	
L_8	0.1	
Н	0.053	
W_1	0.01	
W_2	0.016	

 Tab. 1. The proposed reflectarray unit cell optimized parameters.



Fig. 4. Reflectarray unit element simulation setup in HFSS.

The reflectarray unit cell optimizations are performed using full-wave simulator with periodic boundary conditions and are excited through a Floquet port setup. Angle θ_{ins} is the oblique incidence angle with respect to the normal incidence. The infinite array model is used to calculate the reflection phase response and incident angle effect on the proposed delay-line based structure. Table 1 summarizes different reflectarray parameters.

2.2 Unit Element Performance Parameters

The performance of the proposed unit cell is determined in terms of reflection magnitude, phase range and effect of incident angles in TE and TM modes. The phase range and reflection magnitude plot at 9, 10 and 11 GHz is shown in Fig. 5. Phase range curves at different frequencies are parallel and vary linearly when delay-lines length (θ_s) is varied from 0° to 170°, which shows the wideband property of reflectarray element. A linear and smooth phase range curve ranging about 600° is obtained at X-band center frequency of 10 GHz.

The TE and TM modes incident angle effect at 0° , 15° and 30° is shown in Figs. 6(a) and (b). The incident angle has a little influence on the phase range curve of circular delay-line element. The phase range of simple notched square patch is less than 360° . The phase range of reflectar-ray cell should be greater than 360° [1]. The phase range plot



Fig. 5. Reflection magnitude and phase range at 9, 10 and 11 GHz, where θ_s is the delay-line length.



-600-700 0 25 50 75 100 125 150 175 $\theta_{\rm S}$ (deg)

(b) TM mode oblique incidence at 10 GHz.

Fig. 6. Reflectarray unit cell TE and TM mode phase range, where θ_s is the delay-line length.



Fig. 7. Phase range with and without delay-lines at 10 GHz, where θ_s is the delay-line length and *L* is square length.

with and without delay-lines is shown in Fig. 7. A broad linear phase range is achieved by attaching delay-lines to a notched square. The effect of substrate thickness is observed in Fig. 8(a), a linear phase curve behavior is observed for thicker substrate. The effect of different design parameters at 10 GHz is analyzed. By increasing the square slot width and square length, phase curve shifts to lower frequencies, shown in Fig. 8(b).



(a) Effect of substrate thickness at 10 GHz, where H is the substrate thickness and θ_s is the delay-line length.



(b) Phase range curve behavior by design parameters, where W_1 is gap in slotted square, L_6 is slotted gap length and L_8 is slotted square width (all parameters in λ_0).

Fig. 8. Parametric analysis at different unit cell parameters.

3. Full Reflectarray Configuration

A 27×27 elements center-fed reflectarray is simulated and measured on a low cost FR-4 substrate. The array elements are etched on the top layer and ground plane is employed at the bottom layer. The distance between array elements is kept at $0.25\lambda_0$ in order to minimize grating lobes [1]. The focal distance (*F*) and aperture size (*D*) of the proposed reflectarray are both $6.75\lambda_0$, which indicates the *F/D* ratio of 1. The required phase distribution on reflectarray elements can be calculated by using (1). The phase equation compensates the spatial phase delays and provides a focused beam in desired direction at 10 GHz.

$$\varphi_{\rm R} = k_0 [d_i - (x_i \cos \varphi_{\rm b} + y_i \sin \varphi_{\rm b}) \sin \theta_{\rm b}].$$
(1)

and

$$d_i = \sqrt{(x_i - x_f)^2 + (y_i - y_f)^2 + z_f^2}$$

where k_0 is free space propagation constant, d_i represents the distance between feed horn center and reflectarray *i*th element, (x_i, y_i) is the unit element position and (θ_b, ϕ_b) the reflectarray main beam direction. The feed horn is placed $6.75\lambda_0$ away for the center-fed arrangement. The phase distribution on reflectarray aperture is shown in Fig. 9. The phase shift plot is used to determine the phase shift value required for each array cell. With the use of phase curve in



Fig. 9. Phase distribution on reflectarray aperture.



Fig. 10. Four element group arrangement to reduce cross polarization.

Fig. 5, the proposed unit element is configured into 27×27 elements reflectarray, operating at 10 GHz. The circular delay-lines based array elements are placed in mirror arrangement to reduce the cross polarization. The delay-lines based reflectarray is composed of groups of four elements, where each element of a group is the mirror of its neighbor along both x and y axis. The four element group is shown in Fig. 10 which is repeated in both x and y directions to form a 27×27 elements reflectarray.

3.1 FEBI Based System Simulations

The complete reflectarray system simulations are carried out through hybrid Finite Element Boundary Integral (FEBI) method incorporated in the HFSS software [18]. This method combines the Finite Element Method (FEM) and Integral Equation (IE) and offers faster computation for large sized structures. The 3D-FEBI based reflectarray model is shown in Fig. 11. The feed horn and reflectarray elements are surrounded by two independent radiation boxes. The FEM is applied to the internal structures and IE is assigned to the outer surface of the boxes [14].

The reflectarray model consists of finite number of elements. These elements have different sizes according to phase distribution on array aperture. The radiation patterns computed through FEBI based simulation are more reliable because finite element array configuration is used instead of infinite approximation. The simulation thus caters for the edge effect, incident angles and feed horn position. This method reduces the simulation time and computational re-



Fig. 11. FEBI based system simulations of actual reflectarray.

sources. An HP Z840 workstation with 64 GB RAM takes about 15 hours for full reflectarray FEBI simulation.

3.2 Fabrication and Measurement Results

In order to validate the simulated results, a center-fed reflectarray is fabricated on FR-4 laminate. The proposed unit elements are placed on the top layer with periodicity of $0.25\lambda_0$ and ground plane is placed at bottom layer. The fabricated reflectarray prototype is presented in Fig. 12 (a).

A square wooden stand is manufactured to hold the reflectarray antenna, as shown in Fig. 12(b). The front side is designed to hold the feed horn antenna while reflectarray elements are placed on the rear side of the wooden stand. A Lucas Nuelle[®] WR-90 horn antenna is used as feed anten-



(a) Fabricated reflectarray prototype.



(b) Fabricated reflectarray under testing.

Fig. 12. Reflectarray prototype and testing environment.

na. The horn antenna operates in X-band (8–12 GHz) with 10 dBi gain. The wooden and Acrylonitrile Butadiene Styrene (ABS) material is used for the testing jig to minimize the reflections in the measurement setup. The reflectarray antenna measurements were made in an anechoic chamber. Agilent N5242A PNA-X network analyzer was used for testing of the proposed reflectarray design. Radiation patterns and gain have been measured using Diamond Engineering setup in anechoic environment.

The proposed reflectarray configuration is measured under normal and oblique incident angles. For the proposed reflectarray configuration, TM and TE mode radiation patterns are similar. Therefore, only TE mode normal and oblique incident angle radiations patterns are included in the manuscript. The normalized simulated and measured far-field radiation patterns of the proposed reflectarray in two major planes (E and H) are portrayed in Figs. 13 and 14. The side-lobe-levels are below -25 dB in both planes. The highest value of cross-polarization is at least 40 dB lower than co-polarization at 10 GHz frequency. The simulated and measured half-power beam-width is 15° at 10 GHz.



Fig. 13. Normalized radiation patterns under normal incidence at 10 GHz (TE mode).

The simulated and measured gain against frequency is shown in Fig. 15. A gain maximum of 24.5 dBi is achieved at 10 GHz frequency with aperture efficiency of 49.5%. The measured 1-dB gain bandwidth of the proposed reflectarray antenna is 12.5%, in 9.5 to 10.75 GHz band. The 3-dB measured gain bandwidth is 34%, from 8.45 to 11.85 GHz. The measured gain is slightly lower than simulated due to the wave blockage effect caused by the support structures of feed horn and measurement system imperfections. The performance of delay-lines reflectarray is better than other reflectarrays in terms of side-lobes-levels, cross polarizations and aperture efficiency. The comparison is shown in Tab. 2.



Fig. 14. Normalized radiation patterns at 10 GHz under oblique incident angles at 15° and 30° (TE mode).



Fig. 15. Gain versus frequency.

Reference No.	Current work	[8]	[11]	[15]	[17]
Center frequency (GHz)	10	7.25	10	5.8	10.2
Phase shifting mechanism	Delay- lines	Length variation	Size variation	Different size elements	Size variation
1-dB gain BW (%)	12.5	8.1	18	-	26
3-dB gain BW (%)	34	19.8	-	12	12
Gain (dBi)	24.5	23.7	26.1	22	19
Aperture efficiency (%)	49.5	36	40.3	-	35
F/D	1	0.85	1	-	0.9
No. of array elements	729	121	729	169	52
Unit element phase range	600°	360°	325°	500°	600°
Cross polarization levels (dB)	-40	-20	-23	-20	-21
Side-lobe- levels (dB)	-25	-	-16	-18	-14
No. of layers	1	1	1	2	2

Tab. 2. Comparison with other related works.

4. Conclusion

A single layer reflectarray for X-band applications is presented in this paper. The reflectarray unit cell comprises of diagonally notched square patch attached to circular delay-lines. The unit cell has compact size of $0.25\lambda_0$ designed on low-cost FR-4 substrate. A linear phase range covering 600° is achieved by simply changing the length of circular delay-lines. The proposed unit cell is angularly stable in TE and TM modes, up to 30°. A 27×27 elements reflectarray is simulated, fabricated and measured. The reflectarray has Feed-to-Diameter (F/D) ratio of 1. The measured results shows that 24.5 dBi of gain at 10 GHz is achieved. The simulations and measurements show the proposed antenna has 1-dB bandwidth of 12.5% from 9.5 to 10.75 GHz. The measured cross-polarization and sidelobe-levels are below -40 dB and -25 dB, respectively. The measurement results ensure that the proposed reflectarray is a suitable candidate for high gain X-band applications.

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