Excitation of a Conducting Cylinder Using the Theory of Characteristic Modes

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Abstract. This paper describes the application of the theory of characteristic modes to excite a conducting cylinder representing the chassis of a rocket. Mode excitation is achieved by cutting H-shaped slots on the cylinder at specific locations where the maximum of modal current distribution occurs. The L-matching network is designed to match the impedance of the slots to the input coaxial cable. Finally, the proposed concept is verified during manufacturing and measurement. It is shown that the measured results are in excellent agreement with the simulation.

Keywords

Theory of characteristic modes, coupling elements, matching network

1. Introduction

The development of antennas for rocket communication systems offers interesting research opportunities in the field of antennas because it is crucial that the transmission of telemetry data from the rocket reaches the ground station. There are several experiments in the designing of antennas for rockets that have been conducted where different types of antennas have been discovered, e.g. printed broadband [1], microstrip [2] and blade [3] antennas. However, it is also essential to ensure that the antenna shape should not disturb the aerodynamics of the rocket [4].

In a rocket application, directional antennas are generally mounted in arrays around the body of a rocket [5] or a wrap-around antenna is used [6] in order to obtain an omnidirectional radiation pattern. Instead of mounting antenna arrays on the rocket, we can use its body as the antenna directly. The inspiration comes from the technology of mobile phones which use the chassis of a printed circuit board (PCB) as the main radiating element [7], [8]. Similarly, the authors use the vehicle body as the main radiator in [9], [10]. To the best of our knowledge, the use of the rocket body as a radiator has not been conducted. Hence, this paper demonstrates the proposed concept of how a rocket chassis (essentially modelled as a perfectly conducting cylinder) can be excited while also acting as an effective radiator. The theory of characteristic modes (CM) is used to find the resonant modes of the rocket chassis [11–15]. Since the modes have orthogonal radiation patterns, several frequencies related to the resonance of the modes can be used simultaneously in the telemetry system of the rocket.

In this paper, the model of the rocket represented as a conducting cylinder has been simulated using CST's CM solver [16] to obtain the characteristic modes. Then the first two modes are studied and excited by utilizing the inductive coupling elements implemented by cutting H-shaped slots on the cylinder. CST's time-domain solver is used for this purpose. Both of the modes, especially the first, are suitable to be applied to the rocket due to a simple current distribution and radiation pattern as well as in the use of fewer slots for excitation. A matching network is designed to match the impedance of the slots to the input 50Ω coaxial cable. Finally, the measured results of a fabricated structure with the first mode excited shows excellent agreement with the simulation.

2. The CMs of a Conducting Cylinder

The theory of characteristic modes was originally developed by Garbacz [11] and later refined by Harrington and Mautz [12]. The method of moments [17] complex impedance matrix $\mathbf{Z} = \mathbf{R} + j\mathbf{X}$ is decomposed into a set of characteristic currents \mathbf{J}_n and characteristic numbers (eigenvalues) λ_n by solving the following weighted eigenvalue equation [12]

$$\mathbf{X}\mathbf{J}_n = \lambda_n \mathbf{R}\mathbf{J}_n. \tag{1}$$

Note that the characteristic currents J_n on the surface of a perfect electric conductor (PEC) body depend only on its shape and frequency, not on any specific excitation. The eigenvalues λ_n represent the ratio of reactive to radiated power [18], and hence, if λ_n is zero, the *n*-th mode is in resonance. For better dynamics of the resulting graphs, the characteristic angle [14] is usually plotted as

$$\alpha_n = 180^\circ - \tan^{-1}\lambda_n \tag{2}$$

where $\alpha_n = 180^\circ$ indicates the resonance of the *n*-th mode. In the CST model, the rocket is modelled as a hollow pipe (cylinder) made of PEC material with length L = 1 m, and diameter d = 0.1 m. Number of surface meshcells in the CST integral solver is around 1500. If the pipe is considered to be a thin dipole, one may guess that the first two resonances are at $f_1 \approx c_0/2L = 150$ MHz and $f_2 \approx c_0/L = 300$ MHz, where c_0 is the velocity of light in a free space. In this case, where a relatively thick pipe with L/d = 10 is used, the frequencies are lowered slightly to 129 MHz and 276 MHz, respectively, as shown in Fig. 1.

The characteristic currents of PEC cylinder together with their radiation patterns are shown in Fig. 2. The arrows schematically show the direction of the currents and the black rectangles indicate the position of the inductive couplers, which are discussed later. Obviously, the first mode has a sinusoidal in-phase shape, while the second has two opposite-phase currents resulting in two lobes.



Fig. 1. Variation of the characteristic angle with frequency for the first two characteristic modes of the conducting cylinder.



Fig. 2. The first two characteristic currents and directivity patterns at their resonant frequencies (129 MHz and 276 MHz) of the conducting cylinder.

3. Excitation of CMs

The excitation of modes can be conducted by using inductive coupling elements (ICE). Based on investigations in [7], [8], ICEs are created by cutting small slots at locations where the maximum of characteristic current distributions occur. Therefore, mode 1 can be excited by an inductive coupler at the centre of the cylinder. On the other hand, the characteristic currents of mode 2 flow in opposite directions with two specific maximums. In this case, the mode can be excited by two inductive couplers with a 180° phase shift. The position of the couplers is schematically shown as black rectangles in Fig. 2.

3.1 Excitation of CMs using H-Shaped Slots

To avoid disturbing the distribution of characteristic modes and to maintain the mechanical stability of the design, the ICEs (slots) should be small. In turn, such slots will have low input impedance resulting in problems with matching to 50 Ω . In the CST simulations, slots with various shapes were investigated and, based on the results, the H-shaped slot was found to be the preferable solution from an impedance and compactness point of view, see Fig. 3 left. Mode 1 is excited using two in-phase fed H-shaped slots mounted in the middle of the cylinder on its opposite sides (see Fig. 3 right), which helps to obtain a radiation pattern with good azimuthal symmetry.

Mode 2 is excited using two opposite H-shaped slots in the upper part and two opposite H-shaped slots in the lower part of the cylinder. The current distribution and radiation pattern for both properly excited modes is shown in Fig. 4. Calculated maximum directivies are 1.9 dBi and 2.7 dBi for mode 1 and 2, respectively. By comparing with Fig. 2 it is seen that the slots have negligible effect on the far field pattern.



Fig. 3. Dimensions of the H-shaped slot and their location for excitation of mode 1.

The excitation mechanism of a modal current is seen in Fig. 5. The currents flowing around the left and right parts of the H-shaped slot have opposite directions and thus do not contribute to the far field. It is dominantly the current in the middle that effectively turns on the mode.

The length and width of the vertical arms of the H-shaped slots are $L_v = 100 \text{ mm}$ and $W_v = 23.2 \text{ mm}$, those of the horizontal arms are $L_h = 72.4 \text{ mm}$ and $W_h = 4 \text{ mm}$, and $L_a = 48 \text{ mm}$. The longer the length of either L_v or L_h , the higher the impedance. The wider the width W_v , the higher the impedance as well. In contrast, narrowing W_h results in higher impedance, which explains why W_h is designed to be very thin. Particularly, the impedance of the slots at resonant frequencies of mode 1 and mode 2 are $Z_{\text{mode1}} = 2.69 + j44.36 \Omega$ and $Z_{\text{mode2}} = 17.39 + j129.22 \Omega$, respectively. The driven simulation is performed by using the time-domain CST solver with number of mesh cells of around two million.



Fig. 4. Current distribution and directivity patterns for excited modes 1 (left) and 2 (right). The arrows schematically show the direction of currents. Mode 1 is excited using two in-phase slots, while mode 2 is excited using two pairs of out-of-phase slots (notice the signs +/- representing the phase of the feeding ports).



Fig. 5. Dashed arrows represents currents that cancel each other out while the solid arrow is the dominant path that turns on the modal distribution.

¹Resonant frequency is essentialy given by the length of the cylinder.

For simplicity of design and ease of manufacturing, we further consider the feeding of only mode 1. By CM analysis, it is confirmed that the slot has very little effect on the resonant frequency of the cylinder¹, as shown in Fig. 6 where the resonant frequency is 125 MHz with slots, compared to 129 MHz for the whole pipe.

3.2 Matching the Slots

Considering the excitation of mode 1, there are two slots which have to be connected in parallel to feed them inphase. There are several possibilities as to how to construct the matching network [19]. In our design we use shunt and series capacitors together with RG58C/U phasing cables as shown in Fig. 7.

The length of the cables was set to 200 mm and the values of the capacitors were optimized using a schematic tool in CST Studio with the final (rounded) values C1 = 12 pF in series and C2 = 15 pF in parallel. The mechanical arrangement is shown in Fig. 8. For simplicity of construction, we have not used symmetrization like in [20].



Fig. 6. Characteristic angles of mode 1 with and without slots.



Fig. 7. Matching circuit consisting of shunt and series capacitor and phasing cables (two yellow blocks). The ports 1 and 2 corresponds to that in Fig. 3 right.



Fig. 8. Detailed view of the matching circuit with capacitors, cables and input SMA connector.

4. Measurement

S-parameters at the input SMA connector were measured in an anechoic chamber by the Rohde & Schwarz ZVA 40 [21] vector network analyzer. Despite the handmade design, the simulated and measured input return loss agree very well, as shown in Fig. 9. In particular, there is a 20 dB return loss at the resonant frequency of the first mode (125 MHz from Fig. 6). It is noted that there is another small peak around 470 MHz, which is likely caused by additional resonance caused by the wires connecting the capacitors.

Unfortunately, the frequency of design is too low to measure the radiation pattern in such a chamber. On the other hand, we had to choose an operating frequency accordingly to the pipe length and diameter routinely found in the market place. Taking into account the agreement between simulated and measured matching, one can also expect agreement for the radiation pattern.



Fig. 9. Simulated and measured S-parameters.

5. Conclusions

The excitation of a conducting cylinder using inductive couplers has been presented in this paper. The investigation of the excitation of a rocket chassis as an effective radiator is conducted by the theory of characteristic modes. It was shown that properly designed slots have negligible effect on resonant frequency and current distribution. Although the rocket is modeled in a very simple manner, the presented proof-of-concept indicates that this method can be used in more complex real designs.

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