Simulation of Electrical Characteristics of Switching Nanostructures "Pt – TiO – Pt" and "Pt – NiO – Pt" with Memory

Daulet SERGEYEV¹,², Nurgul ZHANTURINA¹

¹ Dept. of Physics, K. Zhubanov Aktobe Regional State University, Moldagulova Street 34, 030000 Aktobe, Kazakhstan
² Dept. of Radio Electronics, T. Begeldinov Aktobe Aviation Inst., Moldagulova Street 39, 030012 Aktobe, Kazakhstan

serdau@rambler.ru, serdau@mail.ru

Submitted January 1, 2019 / Accepted September 26, 2019

Abstract. The nanostructures “Pt – TiO – Pt” and “Pt – NiO – Pt” with weak switching properties and memory were studied within the framework of semi-empirical Hückel method. The calculation was implemented in the program Atomistix ToolKit with Virtual NanoLab. The transmission spectra, current-voltage characteristics and differential conductivity of nanostructures are calculated.

It was revealed that in the range of voltages –1.3 V÷1.3 V, a hysteresis appears in the form of eight shaped figure on the current-voltage characteristic of Pt – TiO – Pt nanostructure, and in Pt – NiO – Pt nanostructure, the hysteresis appears in the voltage intervals –1.8 V÷0.8 V and 0.9 V÷1.8 V in the form of two oval-shaped figures connected to a segment. The manifestation of the hysteresis characteristic of these nanocontacts shows that they have memory. It was found that a negative differential resistance is observed in the voltage range, where the hysteresis of the current-voltage characteristic is appeared. It is shown that the investigating nanostructures have weak switching properties. The results of the paper can be useful for the calculation of memristic elements of nanoelectronics.

Keywords

Memristor, nanostructure, electron transport, current-voltage characteristic, differential conductivity, transmission function (spectrum)

1. Introduction

At the end of 2008, the discovery of the effect of memrisivity in systems Pt – TiO² – TiO₂ₓ₋₁ – Pt, predicted back in 1971 by L. Chua, became a turning point in microelectronics [1–3]. It became clear that the effect of memrisivity arises in metal-dielectric nanocomposites due to the displacement of charges in a superthin dielectric layer when an electric field is applied. Increased interest in such nanostructures is associated with their use to create a new passive element of the electrical circuit – a memristor – a resistor with controlled resistance. Currently, the creation of switches, memory elements, constituent logic elements, oscillators, as well as modules of neural computers is being considered on the basis of memorial constructions [4–8]. In this regard, there is an intensive search for new metal-dielectric materials with memristive properties, as well as new models, describing their electrical characteristics [9], [10].

Various methods and modeling tools, such as SPICE (LTspice, Multisim and others), FEKO, MatLab, Verilog-A and others [11–15] have been developed to describe the memorial properties of various metal-dielectric materials.

In this paper, an attempt has been made to determine the main electrical characteristics of nanostructures of the type “Pt – TiO – Pt” and “Pt – NiO – Pt” using the extended Hückel method [16].

2. Description of the Object and Methods of Research

The geometry of the studied nanocontacts is shown in Fig. 1, 2 (a), (b). The nanosystems under consideration consist of 306 atoms and have three regions with a total size ~50 Å: central region, left and right electrode areas. In the central region of Pt – TiO – Pt the active part of the nanodevice in the form of an oxide fragment of titanium consisting of 90 atoms is located, and in Pt – NiO – Pt there is nickel oxide consisting of 54 atoms, where the scattering of quasiparticles occurs in a region with a length of ~8.78 Å and ~3.98 Å, respectively. Electrodes are obtained by expanding the central region along the C axis by ~5.73 Å and ~8.6 Å. The distances between electrodes are ~33.24 Å (Pt – TiO – Pt) and ~34.6 Å (Pt – NiO – Pt), where the central region of the nanosystem is located.

Usually, optimization of such structures is well implemented using the ReaxFF potential (ReaxFF is Reactive Force Field), which is used to describe reactive processes [17]. In our case, the optimization of the nanostructures Pt – TiO – Pt is realized using the potential ReaxFF_CHONSiPtZrYBaTi_2013 [18], and of the nano-
structures Pt – NiO – Pt by ReaxFF_CHONSFPt-CNi_2010 [19]. At optimization of Pt – TiO – Pt structure the distance between atoms takes the following values: Pt – Pt ~2.482 Å; Ti – Ti ~2.866 Å; O – O ~2.866 Å; Pt – O ~2.2 Å; Ti – O ~2.195 Å; Pt – Ti ~2.99 Å. In the optimized structure of Pt – NiO – Pt nanocontact, the interatomic distances take the following values: Pt – Pt ~2.58 Å; Ni – Ni ~2.85 Å; O – O ~2.81 Å; Pt – O ~1.758 Å; Ni – O ~2.02 Å; Pt – Ni ~2.72 Å. (The distance and angles between atoms were determined using the VESTA program (Visualization for Electronic and STructural Analysis) [20]).

Computer simulation of the nanocontact was carried out within the framework of the extended Hückel method using the method of nonequilibrium Green's functions (NEGF – Non-Equilibrium Green's Functions) [16]. The calculation of electrotransport properties of the nanocontact consists of two stages. In the first stage, a self-consistent calculation is performed for platinum electrodes in the direction of the flow of electric current. In the second stage, the density matrices are determined, the density of real space is estimated, and the Hartree potential is calculated. A detailed description of this method can be found in [21–23].

To calculate the density matrix of the central region, firstly, a self-consistent calculation of the nanocontact left and right electrodes is performed and the corresponding Fermi levels are estimated: $\varepsilon_L$ and $\varepsilon_R$. Taking into account the bias voltage between two platinum electrodes, we determine the left and right chemical potentials: $\mu_L = \varepsilon_L - eV_{\text{bias}}$ and $\mu_R = \varepsilon_R$. The applied bias voltage moves the quasiparticles from the left electrode to the right, thereby causing an electric current from left to right. The density matrix of the considered nonequilibrium system is represented as the sum of the density matrices of the left and right electrodes:

$$D = D^L + D^R$$  \hspace{1cm} (1)

where $D^L, D^R$ is density matrix of the left and right electrodes, respectively.

$$D^L = \int \rho^L(\varepsilon) f\left(\frac{\varepsilon - \mu_L}{k_B T_L}\right) d\varepsilon$$  \hspace{1cm} (2)

where $\varepsilon$ is energy, $\rho^L(\varepsilon)$ is spectral matrix, $f(\varepsilon)$ is Fermi energy distribution function of quasiparticles, $k_B$ is Boltzmann constant, $\mu_L$ is electrochemical potential, $T_L$ is current temperature of the left electrode. Density matrix for the right electrode $D^R$ is found in a similar way. The spectral matrix is defined using the Green functions:

$$\rho^L(\varepsilon) = \frac{1}{2\pi} G(\varepsilon) \Gamma^L(\varepsilon) G^L(\varepsilon)$$  \hspace{1cm} (3)

where $\Gamma^L(\varepsilon)$ is broadening matrix (broadening function), $G(\varepsilon), G^L(\varepsilon)$ is retarded and advanced Green’s functions. The broadening matrix of the left electrode is described by the following equation:

$$\Gamma^L(\varepsilon) = \frac{i}{\varepsilon} \left[ \mathbf{S}^L - \left( \mathbf{S}^L \right)^* \right]$$  \hspace{1cm} (4)

where $i$ is imaginary unit, $\mathbf{S}^L$ is self-energy of the left electrode. A similar equation exists for the density matrix of

---

**Fig. 1.** The geometry of Pt – TiO – Pt nanocontact: (a) ZX-plane; (b) ZY-plane.

**Fig. 2.** The geometry of Pt – NiO – Pt nanocontact: (a) ZX-plane; (b) ZY-plane.
the right electrode. Green's retarded function is represented as
\[ G(\varepsilon) = \left[ (\varepsilon + i\delta)S - H + \sum_{\ell} R(\varepsilon) - \sum_{R} \right]^{-1} \]  
where \( \delta \) is an infinitely small positive number, \( S \) is overlap integral matrix, \( H \) is Hamiltonian matrix.

After obtaining a self-consistent one-electron Hamiltonian, the transmission function of the nanostructures under consideration is determined, which is then used to determine its current-voltage characteristic (CVC) and differential conductivity. The fraction of the scattering state \( k \), propagating through the structure, is determined by the transmission amplitude \( t_k \), then the transmission coefficient at energy \( \varepsilon \) is determined by summing the transmission amplitude \( t_k \) from all states at this energy:
\[ T(\varepsilon) = \sum_k t_k^* \delta(\varepsilon - \varepsilon_k) \]  
where \( \varepsilon \) is energy, \( t_k \) is transmission amplitude, \( \delta(\varepsilon) \) is delta function. Using (4)–(6), the transmission spectrum can be calculated by the expression:
\[ T(\varepsilon) = \text{tr}\left[ \Gamma^L G^R G^T \right] = \text{tr}\left[ \Gamma^R G^L G^T \right]. \]  

The current flowing through the nanocontact is determined on the basis of the well-known Landauer equation, which indicates the fundamental connection of the electric current with the transmission spectrum:
\[ I = \frac{2e^2}{h} \int_{-\infty}^{\infty} T(\varepsilon) \left[ f\left( \frac{\varepsilon - \mu_R}{k_BT_R} \right) - f\left( \frac{\varepsilon - \mu_L}{k_BT_L} \right) \right] d\varepsilon \]  
where \( e \) is electron charge, \( h \) is Planck's constant, \( T_R, T_L \) are current temperatures and \( \mu_R, \mu_L \) are chemical potentials of the right and left electrode.

The transconductance estimate is obtained by calculating a self-consistent current at a number of applied bias voltages \( V^1_{\text{bias}}, V^2_{\text{bias}}, ... \), and performing numerical differentiation according to the formula
\[ \sigma(V_{\text{bias}}, T_L, T_R) = \frac{I(V^1_{\text{bias}}, T_L, T_R) - I(V^2_{\text{bias}}, T_L, T_R)}{V^1_{\text{bias}} - V^2_{\text{bias}}}. \]  

\[ \text{Fig. 3.} \text{ Evolution of the transmission spectra of “Pt – TiO – Pt” (a) and “Pt – NiO – Pt” (b) nanocontacts with an increase in the bias voltage \( V_{\text{bias}} \) from -3 V to 3 V.} \]
Fig. 4. Evolution of the transmission spectrum $T(k)$ of Pt - TiO - Pt nanocontacts with a change in energy: (a) –1.32 eV; (b) –0.96 eV; (c) 0 eV; (d) 2.88 eV; (e) 3.48 eV; (f) 5.52 eV.

and $k_B = -0.0011$. As can be seen, the transmission spectrum of the structure is an oscillating function.

Figure 5 shows the evolution of the transmission spectrum of Pt – NiO – Pt nanocontact from $k$ with a change in energy. As can be seen from Fig. 3(b) the oscillation of the transmission spectrum occurs in the energy interval $–4.2$ eV÷0 eV; therefore, we consider the dependence $T(k)$ in this energy interval. At $–4.2$ eV, four localized maxima of the spectrum are observed (Fig. 5a). With increasing energy up to $–2.4$ eV, the peak values of the spectrum accumulate at the center of the dependence $T(k) = 14$ arb. units at $k_A = k_B = 0$. Further, the maxima of $T(k)$ function begin to shift from the center to the edge and at $–1.2$ eV the minimum value of the spectrum is observed at $k_A = k_B = 0$.

The results of simulation of current-voltage characteristics (CVC) and differential conductivity are shown in Fig. 6. (The solid curve describes the characteristics of the direct connection of nanocontacts to the power source, and the dotted one – on the reverse inclusion.)

In the voltage range of $–1.3$ V÷1.3 V, when directly connected and changing the polarity, the CVC characteristic of Pt – TiO – Pt nanocontact acquires a shape of eight number (inherent in memristive elements). However, with further voltage variation, no hysteresis of the current-voltage characteristic is observed (Fig. 6a).

The differential conductivity of such nanosystem has a peak structure, and when directly turned on, its maxima of 260 µS, 60 µS, 120 µS are observed at values of a bias voltage of 0 V, ± 1.4 V, ± 2.6 V, respectively. The minima of the $dI/dV$ spectrum of the nanosystem $–30$ µS and $20$ µS occur as “dips” at bias voltages of ±1 V, ±1.8 V, respectively. When the nanocontact is switched back on, the “large peak” of conductivity splits into two 222 µS and 250 µS at voltages of –1.1 V and 1.2 V, respectively (Fig. 6a).

The hysteresis of the CVC of Pt – NiO – Pt nanocontact is observed in the voltage range of $–1.8$ V÷0.8 V and 0.9 V÷1.8 V in the form of an oval shape (Fig. 6 b). Outside the specified voltage range, the amount of current flowing through the contact is the same in both direct and reverse connection.

At direct and reverse switching of the nanocontact, the maxima of the differential conductivity of 300 µS and 270 µS appear at a bias voltage of $–2$ V and 2.1 V, respectively, also “secondary” peaks 110 µS and 125 µS occur at ±1.05 V.

Differential conductivity dips are observed at $–2.6$ V ($–12$ µS), $–1.6$ V ($–70$ µS), 1.6 V ($–30$ µS), 2.4 V (36 µS). At reverse switching, a shift in dips of $–1.4$ V ($–50$ µS), 1.45 V ($–20$ µS) is observed.

As can be seen from Fig. 6(a), (b), on the characteristics of both nanocontacts, a negative differential resistance
Fig. 5. Evolution of the transmission spectrum $T(k)$ of Pt - NiO - Pt nanocontacts with a change in energy: (a) –4.2 eV; (b) –3.36 eV; (c) –2.4 eV; (d) –1.2 eV; (e) –0.36 eV; (f) 0 eV.

Fig. 6. Current-voltage and $dI/dV$ characteristics of Pt – TiO – Pt (a) and Pt – NiO – Pt (b) nanocontacts: solid curve – direct connection, dashed – reverse connection.

is observed in the voltage range, where the hysteresis of the CVC is appeared.

Observation of the hysteresis characteristics of these nanocontacts shows that they have memory. Also, from the current-voltage characteristics of the structures, it can be seen that the investigated objects have weak switching properties (Fig. 6). For example, at reverse connection of Pt – TiO – Pt nanocontact in the voltage range of $-0.86 \text{ V} \sim 1 \text{ V}$, a rapid linear change in the current value from $-42 \mu\text{A}$ to $42 \mu\text{A}$ is observed, and in the case of Pt – NiO – Pt nanocontact, switching from ON mode to OFF occurs at voltages of $-0.88 \text{ V}$ and $0.85 \text{ V}$.

Figure 7 shows the hysteresis of the CVC and the change in the resistance of the channels of nanocontacts depending on the bias voltage. As can be seen, at the beginning of the formation of hysteresis, the CVC of the nanocontacts of the channel resistances for direct and reverse connection are ($R_{d.c.0} \approx R_{r.c.0}$).

At the case of nanocontact Pt – TiO – Pt: $R_{d.c.0} \approx R_{r.c.0} \approx 12.9 \text{ k}\Omega$. At direct switching of nanocontact Pt – TiO – Pt in the interval of $V_{bias}$ from $-1.3 \text{ V}$ to $0 \text{ V}$ channel resistance decreases exponentially to several ohms, then in the interval $V_{bias}$ from $0 \text{ V}$ to $1.3 \text{ V}$ its value is restored (Fig. 7 a). At reverse switching of nanocontact in the
interval of $V_{\text{bias}}$ from $-1.3$ V to 0.1 V resistance increases to 95.24 kΩ. Then there is a sharp decrease in channel resistance and at the same time the completion of the first loop of the CVC. A similar inverse process of resistance behavior during reverse switching occurs in the interval of $V_{\text{bias}}$ from 0 V to $-1.3$ V, forming the second loop of CVC.

At the beginning of the formation of hysteresis of the CVC of the nanocontact Pt – NiO – Pt the resistances $R_{\text{d.c.0}} \approx R_{\text{r.c.0}} \approx 23.74 \Omega \div 24 \Omega$. At direct switching of the nanocontact in the interval $V_{\text{bias}}$ from –1.8 V to –1.3 V channel resistance decreases to 16 kΩ, then in the interval of $V_{\text{bias}}$ from –1.3 V to –0.1 V its value increases to ~41 kΩ (Fig. 7b). Further, the reverse quasi-symmetric behavior of the resistance is observed with a minimum value of ~18 kΩ and at $V_{\text{bias}} \approx 1.8$ V the final resistances at direct and reverse switching are equal to $R_{\text{d.c.1}} \approx R_{\text{r.c.1}} \approx 23.2$ kΩ. The channel resistance increases sharply, forming the maximum value of the first hysteresis loop of the CVC due to the significant difference in resistance $\Delta R = |R_{\text{d.c.}} - R_{\text{r.c.}}| \approx 30.48$ kΩ. Then the channel resistance decreases to 17 kΩ at a near-zero bias voltage value. At $V_{\text{bias}} \approx 0.7$ V, the formation of the first hysteresis loop of the CVC is completed. Then, in the range of $V_{\text{bias}}$ from –0.1 V to –1.35 V, an increase in channel resistance is observed. At $V_{\text{bias}} \approx –0.8$ V, the resistances $R_{\text{d.c.0}} \approx R_{\text{r.c.0}} \approx 25$ kΩ and the second CVC loop is formed. The growth of the channel resistance stops after reaching the maximum value of 65.7 kΩ at $V_{\text{bias}} \approx -1.35$ V. In this case, the value $\Delta R \approx 51.43$ kΩ assumes the maximum value, which is reflected in the hysteresis of the CVC.

4. Conclusion

Thus, in this work, the basic electric transport characteristics (transmission spectra, CVC, differential conductivity) of Pt – TiO – Pt and Pt – NiO – Pt nanocotacts were investigated within the framework of the semi-empirical extended Hückel method. It was shown that in the voltage range $-1.3$ V÷1.3 V, the CVC of Pt – TiO – Pt nanostructure has a number eight shape hysteresis, and the hysteresis of the CVC of Pt – NiO – Pt nanostructure manifests itself in voltage intervals $-1.8$ V÷0.8 V and 0.9 V÷1.8 V in the form of two oval-shaped figures, connected to a segment. Observation of the hysteresis characteristics of these nanocontacts shows that they have memory. It was found that the “large peak” of the differential conductivity of Pt – TiO – Pt nanocontact at the reverse switching of the conductivity splits into two 222 $\mu$S and 250 $\mu$S at voltages of –1.1 V and 1.2 V. It is shown that negative differential resistance is observed in the voltage range, where the hysteresis of the current-voltage characteristic is appeared. The evolution of the transmission spectrum of the nanostructure with an increase in the bias voltage (from –3 V to 3 V) is presented. It is shown that an increase in the difference in the resistance of the channels of nanocotacts increases the hysteresis of their CVC. The results of the paper may be useful for the calculation of new promising memorial elements of nanoelectronics.

References

memristors. Scientific Reports, 2016, vol. 6, p. 1–6. DOI: 10.1038/srep21331


About the Authors ...

Daulet SERGEYEV was born in Kazakhstan, Aktobe, Ph.D., associate professor. He has defended his Ph.D. thesis in 2010. His research interests include modeling of physical processes in solids, nanoelectronics, superconducting electronics, Josephson effect, Andreev reflection, point defects study.

Nurgul ZHANTURINA was born in Kazakhstan, Uralsk, Ph.D. She has defended her Ph.D. thesis in 2014. Her research interests include dynamics of excitons state in solids, electronic excitations in dielectrics, theoretical modeling of physical processes in solids, luminescence.