Isosceles Triangular Resonator Based Compact Triple Band Quad Element Multi Terminal Antenna

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Abstract. A triple band quad element multi-input-multioutput (MIMO) antenna is proposed for Bluetooth (2.4 GHz), WLAN (2.5/4.9 GHz) and LTE (3.7 GHz) applications. A compact triangular ring-shaped structure is used as an antenna element. An isosceles triangular ring resonator is designed in such a way that it offers dual-band and another ring resonator is placed inside the empty space of the first resonator to obtain the third band. The antenna element is studied in terms of $|S_{11}|$ and also the current distributions are observed at three resonance frequencies to find out the resonance mechanism. The proposed quad element MIMO antenna is compact in total area $(0.45\lambda_0 \times 0.45\lambda_0)$. Isolation better than 20 dB is achieved with minimum inter-element spacing of $0.07\lambda_0$ without extra isolation circuit. Gain, radiation patterns, envelope correlation coefficient (ECC), diversity gain (DG), channel capacity loss (CCL) and total active reflection coefficient (TARC) values are studied to comprehend the MIMO performance of the proposed design.

Keywords

Isosceles triangular ring resonator, triple band antenna, MIMO antenna, isolation

1. Introduction

In the present scenario, smart device requires multiple bands with high data rate for different application which can be accomplished by multiple antennas with multiple operating bands like LTE, Bluetooth, WLAN, GPS, GPRS, etc. Multi-input-multi-output (MIMO) antenna becomes the first choice for the makers of communication device to achieve high data rate and less multipath fading effect [1]. However, MIMO antenna need large area in order to reduce the mutual coupling between antenna elements. Thus, it is very important to reduce the inter-element spacing of MIMO antenna to make the device size user friendly without degrading the isolation between ports. Various designs of MIMO antenna are reported in recent years towards compactness of the antenna size. An ultra-wide band antenna is proposed in [2] for MIMO applications and elec-

tromagnetic band gap (EBG) structure is used in order to achieve proper isolation between antenna elements. EBG structure needs via which leads to design complexity. Dualband two element MIMO antenna is presented in [3], slots are etched on ground plane to improve isolation. In [4], a dual element dual-band antenna is proposed for MIMO applications, however, isolation is less in the first band of operation. A multiband MIMO antenna is proposed for C and X band applications in [5], Defected ground structure (DGS) technique is used to enhance the isolation. In [6], T. Kumari et al. proposed a dual band dielectric resonator (DR) based MIMO antenna and DGS technique is used in order to achieve significant isolation. D. Sarkar and K. V. Srivastava proposed a split ring resonator (SRR) based dual band antenna for MIMO applications [7]. A triple band antenna is proposed in [8] and a defect is introduced on ground plane to achieve more isolation. In [9], a triple band MIMO antenna for GSM900/1800 and LTE2600 application is proposed; a winding meandered line structures and T-shaped slot are used in order to enhance isolation. In [10], a two-element triple band MIMO antenna is proposed and it contains one notched band. A modified inter-digital capacitor (MIDC) is introduced in between two antenna elements in order to improve isolation. A circularly polarized two elements MIMO antenna is proposed in [11] in which a grounded slit is used to achieve good isolation. A triple band MIMO antenna is proposed in [12] with independent tunable characteristics. In most of the previous works different type of isolation circuit is introduced to maintain the proper isolation in multiple bands which increases the design complexity.

This paper presents a triple band quad element MIMO antenna for Bluetooth, WLAN and LTE operations with a compact area with proper isolation. The antenna element consists of two triangular split ring resonators, is modeled in such a way that it occupies minimum area. The resonance frequencies are observed at 2.5 GHz, 3.7 GHz and 4.9 GHz. The proposed MIMO gives satisfactory radiation pattern at three resonances with cross polar performance better than 30 dB. Orthogonal arrangement of antenna element provides isolation between two consecutive ports better than 20 dB without using extra isolation network. ECC, DG, CCL and TARC values satisfy the MIMO performances. Simple configuration and compact size with triple band operation and significant performances in MIMO applications reveal its novelty.

Unit element antenna design and analysis are presented in Sec. 2. MIMO antenna design is described in Sec. 3. In Sec. 4, fabrication and measurement results are discussed. Diversity performance is discussed in Sec. 5 and the paper is finally concluded in Sec. 6.

2. Antenna Design and Analysis

The design and analysis of unit element of the MIMO antenna is discussed in this section. Unit element configuration is inspired and extended from authors' previous work given in [13]. A substrate with relative permittivity 4.4, loss tangent 0.02 and 1.58 mm height is chosen to design the antenna and the schematic diagram is shown in Fig. 1. All dimensions are mentioned in Fig. 1. The antenna is fed by a 50 Ω microstrip line through a matching line [12]. The design steps to achieve triple band antenna are elaborated in three steps as shown in Fig. 2(a) and the corresponding $|S_{11}|$ are plotted in Fig. 2(b). In the first step, an isosceles triangular ring resonator (ITRR) is designed as Ant-A, shown in Fig. 2(a) which provides single resonance. Then, a slot is etched on either one of the two equal legs of the ITRR, denoted as Ant-B to achieve dual resonances. Lastly, a modified triangular split ring resonator is placed inside the empty space of the ITRR and the whole structure provides triple band response. First and second bands are shifted towards lower frequency due to the incorporation of the second resonator as there is an electromagnetic coupling between the two resonators. A parametric study is done on Ant-B by varying the slot position. Here, $|S_{11}|$ for



Fig. 1. Schematic of the proposed triple band antenna (w=20, l=25, $l_1=13.2$, $l_2=11$, $w_2=1.5$, $l_3=8$, $l_4=2.75$, $l_5=3$, $l_6=1.1$, $l_7=6.3$, $l_r=4$, $w_r=3$, $g_1=0.25$, $g_2=0.25$, $g_3=0.25$, $t_1=1$, $t_2=0.3$, $t_3=0.25$ (all dimensions are in mm)).

four different slot positions (P_A/P_B/P_C/P_D) and without slot are presented in Fig. 2(c). From this figure, it is observed that a slot at P_A/P_B/P_C generates dual band as the slot makes two different current paths, path-1 and path-2. At resonances, both paths are equal to half guided wavelength ($\lambda_g/2$). It is also noticed that the first band is shifted towards higher frequency and the second band is shifted towards lower frequency when slot position moves from P_A to P_C through P_B. The possible reason could be the length of path-1 is decreased whereas length of path-2 is increased. A slot on apex i.e at P_D is etched and the antenna offers single band as like Ant-A (without slot). However, the resonance is shifted slightly towards lower frequency. Possible reason for this shifting is the capacitive effect for the split on P D.

Current distribution at three resonance frequencies are plotted in Fig. 3(a)–(c) for further confirmation of current path of each resonance. Path-1 is responsible for the first resonance at 2.5 GHz as maximum current is concentrated



Fig. 2. Antenna configuration and response: (a) Design steps.
(b) |S₁₁| of the three antennas. (c) |S₁₁| plot with the variation of slot position for outer ring only.



Fig. 3. Surface current distribution (A/m) at (a) 2.5 GHz, (b) 3.7 GHz, (c) 4.9 GHz.

on path-1 as shown in Fig. 3(a). The second resonance at 3.7 GHz occurred due to the path-2 and the second resonator, evident from the current distribution plot in Fig. 3(b). Figure 3(c) reveals that maximum current is observed on the second resonator which confirms that the second resonator is responsible for generation of the third resonance at 4.9 GHz.

3. Quad Element MIMO Antenna

The triple band antenna discussed in Sec. 2 is used to realize a quad element MIMO antenna as shown in Fig. 4. By virtue of negligible cross-polar level of the unit element, substantial isolation (less than 30 dB) between them can be achieved by placing two consecutive antennas orthogonally, which in turn will mitigate the area of the MIMO antenna. As four elements of the MIMO antenna are symmetric and placed symmetrically, only four S-parameters ($|S_{11}|$, $|S_{21}|$, $|S_{31}|$ and $|S_{41}|$) out of sixteen are presented in Fig. 4(b) by exciting antenna #1. Excitation of the other antenna element provides overlapping S-parameters. From $|S_{11}|$ response of the proposed MIMO antenna, it is verified that resonance frequencies and the operating bandwidth remain almost similar to the unit antenna element. As shown from Fig. 4(b), $|S_{21}|$ and $|S_{41}|$ are similar as antenna element #2 and #4 are positioned identically with respect to antenna element #1.

4. Fabrication and Measurement

To validate the simulation performance of the proposed MIMO antenna, a prototype is fabricated on FR4 substrate of height of 1.58 mm as shown in Fig. 5(a). The S-parameters are measured with the help of a vector network analyzer (Agilent N5230A) and depicted in Fig. 5(b). It is observed that the results are in a good agreement with simulation. The resonances are observed at 2.4 GHz,



Fig. 4. Four element MIMO antenna: (a) Orientation $(l_m = w_m = 55 \text{ mm})$. (b) Simulated S-parameters.



Fig. 5. MIMO antenna: (a) Fabricated prototype. (b) Measured S-parameters.

3.75 GHz, 4.95 GHz with a bandwidth of 300 MHz, 820 MHz and 200 MHz respectively and isolations are better than 20 dB.

Far-field radiation patterns are measured in both XZ and YZ plane and normalized values are plotted in Fig. 6 along with simulated results at three resonance frequencies. The patterns are omnidirectional with good cross-polar performance (better than 25 dB). Gain of 0.6 dBi, 1 dBi and 0.8 dBi are observed at 2.5 GHz, 3.7 GHz and 4.9 GHz frequencies respectively. In Fig. 6(c), a 10° inclination in the radiation pattern at the third resonance is observed due to the excitation of higher order modes of isosceles triangular (outer) resonator.



Fig. 6. Far field radiation patterns at (a) 2.5 GHz, (b) 3.7 GHz and (c) 4.9 GHz.

5. Diversity Performance

Isolation and radiation patterns are not the only parameters to conclude about the performance of a MIMO antenna. Diversity performance plays a big roll to determine the MIMO antenna performance. In this section, diversity performance is discussed in terms of ECC, DG, CCL and TARC. ECC provides information of correlation between the radiation patterns of two antenna elements. ECC can be calculated by the following procedure given in [14].

$$\rho_{\mathbf{e},ij} \cong |\rho_{\mathbf{c},ij}|^{2} = \left| \frac{\int \left(XPR \cdot E_{\theta i} \cdot E_{\theta j}^{*} \cdot P_{\theta} + E_{\phi i} \cdot E_{\phi j}^{*} \cdot P_{\phi} \right) d\Omega}{\left| \sqrt{\int \left(XPR \cdot G_{\theta i} \cdot P_{\theta} + G_{\phi i} \cdot P_{\phi} \right) d\Omega} \right|^{2}} \right|^{2} \cdot$$

$$(1)$$

Here, *XPR*, Ω , $E_{\theta}(\Omega)$, $E_{\phi}(\Omega)$ represent cross polarization power ratio of incident wave, solid angle, θ and ϕ components of active electric field. θ and ϕ components of angular density of incoming plane waves are denoted by P_{θ} and P_{ϕ} . $P_{\theta} = P_{\phi} = 1/(4\pi)$ and XPR = 1 are considered in certain propagation environment. G_{θ} and G_{ϕ} stand for θ and ϕ polarised signal realised active gain patterns. The following equations relate active gain patterns and electric field components: $G_{\theta i} = E_{\theta i} \cdot E_{\theta i}^{*}$, $G_{\theta j} = E_{\theta j} \cdot E_{\theta j}^{*}$, $G_{\phi i} = E_{\phi i} \cdot E_{\phi i}^{*}$, and $G_{\phi j} = E_{\phi j} \cdot E_{\phi j}^{*}$.

So, equation (1) can be written as

$$\rho_{e,ij} = \left| \frac{\iint \left(E_{\theta_i} \cdot E_{\theta_j}^* + E_{\phi_i} \cdot E_{\phi_j}^* \right) d\Omega}{\sqrt{\iint \left(E_{\theta_i} \cdot E_{\theta_i}^* + E_{\phi_i} \cdot E_{\phi_i}^* \right) d\Omega \iint \left(E_{\theta_j} \cdot E_{\theta_j}^* + E_{\phi_j} \cdot E_{\phi_j}^* \right) d\Omega} \right|^2. \tag{2}$$

ECC calculation from far field parameters is very complex and time-consuming process. Broadband ECC can be calculated from S-parameters when it is considered that incoming signal is plane wave and antennas are well matched and lossless [15]. Although S-parameters do not provide any information of radiation pattern, it is significantly accurate when the MIMO antenna is placed in free space. The following equation provides ECC by using S-parameters.

$$\rho_{e,ij} = \frac{|\sum_{n=1}^{N} S_{in}^* S_{nj}|^2}{(1 - |\sum_{n=1}^{N} |S_{ni}|^2)(1 - |\sum_{n=1}^{N} |S_{nj}|^2)}.$$
 (3)

The derived ECC by post processing the simulated and measured S-parameters are shown in Fig. 7 and it is found that the ECC values at three bands are very less compared to diversity thumb rule value of 0.5.



Fig. 7. ECC plots of the proposed antenna.



Fig. 8. Diversity gain plots of the proposed antenna.

Diversity gain refers the signal to noise ratio improvement respect to single antenna. DG is calculated using (4) in [2] and plotted in Fig. 8.

$$DG = 10\sqrt{1 - ECC^2}.$$
 (4)

The calculated DG values from simulated and measured ECC are almost 10 dB which validate the application of this antenna.

Channel capacity loss measures the loss of channel capacity due to the correlation between two antenna elements. Lesser CCL offers better performance and it can be calculated by (5–8) in [2]. The calculated CCL from the simulated and measured data are shown in Fig. 9. This figure reveals that the CCL values are 0.15, 0.12 and 0.25 bits/sec/Hz.

$$C_{\rm loss} = -\log_2(\psi^R), \qquad (5)$$

$$\psi^{R} = \begin{bmatrix} \rho_{11} & \rho_{12} & \rho_{13} & \rho_{14} \\ \rho_{21} & \rho_{22} & \rho_{23} & \rho_{24} \\ \rho_{31} & \rho_{32} & \rho_{33} & \rho_{34} \\ \rho_{41} & \rho_{42} & \rho_{43} & \rho_{44} \end{bmatrix}$$
(6)

where

$$\rho_{ii} = 1 - \left(\sum_{n=1}^{N} |S_{in}^* S_{ni}|\right), \tag{7}$$

$$\rho_{ij} = -\left(\sum_{n=1}^{N} |S_{in}^*S_{nj}|\right), \ i,j,n = 1,2,3,4.$$
(8)

Total active reflection coefficient is one of the significant parameters to understand the merit of MIMO antenna. It provides active bandwidth of MIMO antenna. TARC value is sensitive with the phase difference between the incoming signal at the two ports. The TARC values with some different phase combinations are calculated using (9-11) in [2] presented in Fig. 10.

$$\Gamma_{a}^{\prime} = \frac{\sum_{n=1}^{N} |b_{i}|^{2}}{\sum_{n=1}^{N} |a_{i}|^{2}},$$
(9)

$$[\mathbf{b}] = [\mathbf{S}][\mathbf{a}].$$
 (10)

Here, a_i and b_i stand for incident and reflected wave respectively. **[a]**, **[b]** and **[S]** are incident, reflected and scattering matrix. In Fig. 10, 0°, 120° and 0° means incident



Fig. 9. CCL plots of the proposed antenna.



Fig. 10. TARC values with different phase combinations.

wave at antenna element #2, #3 and #4 are led with 0° , 120° and 0° to the antenna element #1.

$$\begin{bmatrix} b_1 \\ b_2 \\ b_3 \\ b_4 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} & S_{13} & S_{14} \\ S_{21} & S_{22} & S_{23} & S_{24} \\ S_{31} & S_{32} & S_{33} & S_{34} \\ S_{41} & S_{42} & S_{43} & S_{44} \end{bmatrix} \begin{bmatrix} a_1 \\ a_2 \\ a_3 \\ a_4 \end{bmatrix}.$$
(11)

6. Discussions

[Ref], Year	No. of bands/ antenna element	Area $(x\lambda_0 \times y\lambda_0)$	I (dB)	ECC	CCL (bits/s/Hz)	TARC (dB)
[14], 2015	4/4	0.69×0.69	≥20	≤0.009	-	-
[8], 2016	3/2	0.30×0.20	≥16	≤0.7	-	-
[6], 2017	2/4	0.32×0.32	≥20	≤0.009	-	-
[7], 2017	3/2	0.2×0.36	≥15	≤0.01	≤0.4	-
[2], 2018	1/4	0.6×0.6	≥17	≤0.3	≤1.5	≤ -6
[4], 2018	2/2	0.96×1.03	≥18	≤0.21	≤0.25	-
[12], 2018	3/4	0.32×0.32	≥20	≤0.001	≤0.30	-
[16], 2014	2/4	1.39×1.39	-	-	-	-
This work	3/4	0.45×0.45	≥20	≤0.01	≤0.25	≤-8

 Tab. 1. Comparison of the proposed work with published work in literatures.

A comparison of this work with other literatures is tabulated in Tab. 1. From the comparison table, it is observed that only [6] is more compact and offers better ECC than the proposed work. However, [6] is a dual band antenna. Design [4] has the same CCL value with the proposed design, however, it offers dual band with larger size. The antenna [14] has four elements and provides quad band. However, the size of the structure is very large compared to the proposed design. The proposed work offers better performances with respect to [2] in terms of number of bands and TARC values. It is evident that this design is more compact in size with triple band response and reasonably good MIMO characteristics.

7. Conclusion

This paper presents a compact triple band antenna for MIMO applications. A modified triangular ring resonator is placed inside the empty space of a split isosceles triangular ring resonator to realize the triple band response. This antenna element is used further to design a quad element MIMO antenna which offers the bands at 2.35-2.65 GHz, 3.36-4.18 GHz and 4.80-5.00 GHz. Orthogonal arrangement of antenna element provides isolation better than 20 dB between two terminals which makes it suitable for MIMO applications. Diversity performances are studied to check the antenna performance as MIMO applications and these are within the acceptable limit. Radiation patterns of this antenna at three resonances are omnidirectional with a gain of 0.6 dBi, 1 dBi and 0.8 dBi for the first, second and third resonances, respectively. Thus, this antenna is a suitable candidate for Bluetooth (2.4 GHz), WLAN (2.5/4.9 GHz) and LTE (3.7 GHz) applications.

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